

**MATHEMATICS ENGLISH MEDIUM
SET 02 KEY ANSWERS.**

MODEL PAPER-2

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KSEEB SSLC MODEL QUESTIONS PAPER – 02

MATHEMATICS 81 E

QUESTION PAPER & KEY ANSWERS

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MARKS:80

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DURATION: 3 Hours 15min

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. 1x8=8

1. The number of tangents that can be drawn to the circle at the point on its circumference is
 A) Many B) 3 C) 2 D) 1

Solution: D) 1

Explanation: There can be only one tangent at a point on the circle.

2. a and b are the two positive integers, then the correct relationship between the HCF(a, b) and LCM(a, b) is

- A) $HCF(a, b) \times LCM(a, b) = a - b$ B) $HCF(a, b) \times LCM(a, b) = a \times b$
 C) $HCF(a, b) + LCM(a, b) = a + b$ D) $HCF(a, b) - LCM(a, b) = a \times b$

Solution: B) $HCF(a, b) \times LCM(a, b) = a \times b$

3. The number of solutions for the pair of linear equations $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ when $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ is

- A) 0 B) 1 C) 2 D) Infinite

Solution: B) 1

Explanation:

We know that $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$, there is intersecting lines (Only one solution) – consistent lines

$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ Coincident lines (infinitely many solutions) - consistent lines

$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ Parallel lines (No solutions) – Inconsistent lines

4. If nth term of an arithmetic progression is $3n - 1$, then its 8th term is

- A) 25 B) 10 C) 23 D) 12

Solution: C) 23

Explanation: we have $a_n = 3n - 1$ for finding 8th term put $n = 8$.

$$a_8 = 3(8) - 1$$

$$a_8 = 24 - 1 = 23$$

5. The maximum number of zeroes of the polynomial $p(x) = x^3 - 1$ is

- A) 3 B) 0 C) 1 D) 2

Solution: A) 3

Explanation: We know that a linear equation has only one zero

A quadratic equation has two zeroes

A cubic polynomial has 3 zeroes

6. The volume of a right circular based cylinder is 1540 cubic cm and its height is 10cm. the area of its base is

A) 15.4cm B) 15.4cm² C) 154cm² D) 154cm³

Solution: C) 154cm²

Explanation: We know volume of cylinder, $V=1540$

$$\Pi r^2 h = 1540$$

Height is given, $h=10\text{cm}$,

$$\Pi r^2 \times 10 = 1540$$

$$\Pi r^2 = 154 \text{ sq cm}$$

Which is required area of the base of cylinder

7. The formula to find the mean of the grouped data by direct method is

A) $\frac{\sum fx}{\sum f}$ B) $\frac{\sum f+x}{\sum f}$ C) $\frac{\sum f}{\sum fx}$ D) $\frac{\sum f-x}{\sum f}$

Solution: A) $\frac{\sum fx}{\sum f}$

8. $\frac{1-\tan^2 45^\circ}{1+\tan^2 45^\circ}$ is equal to _____ .

A) $\tan 90^\circ$ B) $\sin 45^\circ$ C) $\cos 0^\circ$ D) $\sin 0^\circ$

Solution: D) $\sin 0^\circ$

Explanation: We have $\frac{1-\tan^2 45^\circ}{1+\tan^2 45^\circ} = \frac{1-1}{2} = 0$

Among the options, $\sin 0$ is 0. Hence D is correct answer.

Note: options are also more important

II. Answer the following questions

1x8=8

9. Write the formula to find the sum of first n terms of the arithmetic progression whose first term is a and last term is an.

Solution: $\frac{n}{2} \{a + an\}$

10. Write the coordinates of the midpoints of the line joining the two points A(x₁, y₁) and B(x₂, y₂).

Solution: $\left[\frac{x_2+x_1}{2}, \frac{y_2+y_1}{2} \right]$

11. The pair of linear equations $x+y-4=0$ and $2x+by-3=0$ have no solutions. Find the value of b.

Solution: The value of b is 2

Explanation: We know $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ Parallel lines (No solutions) – Inconsistent lines

$$\frac{1}{2} = \frac{1}{b}$$

$$b=2$$

12. Find the maximum length of the rod to completely measure the rods of the lengths 24m and 36m.

Solution: 12m.

Explanation: we need to find the HCF of both lengths, so HCF is 12.

13. Write the formula to find the surface area of the sphere.

Solution: surface area of the sphere is $4\pi r^2$.

14. If one of the zeroes of the polynomial $p(x)=x^2+7x+k$ is 2. Then find the value of k.

Solution: $K = -19$

Explanation: One zero is 2

$$\begin{aligned} \alpha &= 2 \text{ we know } \alpha\beta = \frac{c}{a} \\ 2 \times \beta &= \frac{k}{1} \\ 2\beta &= k \end{aligned}$$

Sum of its zeroes $\alpha + \beta = \frac{-b}{a}$

$$2 + \beta = \frac{-7}{1} \text{ then } \beta = -9$$

Then $k = 2 \times -9 = -18$

15. Find the value of the discriminant of the quadratic equation $x^2+4x+4=0$

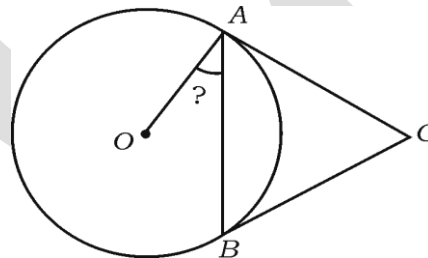
Solution: discriminant is 0

Explanation: we know that discriminant, $\Delta = b^2 - 4ac$

$$\begin{aligned} &= 4^2 - 4 \times 1 \times 4 \\ &= 16 - 16 = 0 \end{aligned}$$

16. In the given figure, O is the centre of the circle and CA and CB are the tangents to the circle. If $AB=AC$ then find the measure of $\angle OAB$.

Solution: $\angle OAB = 30^\circ$.



Explanation: Given that $AB=AC$, Then $BC=AC$ because it is tangents.

Hence triangle ABC is an equilateral triangle.

We know $\angle OAC=90^\circ$, if triangle ABC is an equilateral triangle then $\angle BAC=60^\circ$

If $\angle BAC=60^\circ$, then $\angle OAB = 90 - 60 = 30^\circ$

III. Answer the following questions

2x8=16

17. Find the sum of first 20 terms of an A.P 4, 7, 10,

Solution: Given data here $a=4$, $d=7-4$ $n=20$
 $d=3$

We are going to find S_{20}

We know $S_n = \frac{n}{2} \{2a + (n - 1)d\}$

$$\begin{aligned} S_{20} &= \frac{20}{2} \{2 \times 4 + (20 - 1)3\} \\ &= 10 \{8 + (19)3\} \\ &= 10 \times 65 \\ &= 650. \end{aligned}$$

18. Solve $2x+y=8$ and $x-y=1$.

Solution: we have $2x+y=8 \rightarrow (1)$

and $x-y=1 \rightarrow (2)$

By elimination method $2x+y=8$
 $x-y=1$

by subtracting above two we get $3x=9$ **$x=3$**

Put this x value in any one of the above equation we get **$y=2$**

OR

The difference between two positive numbers is 26 and if one number is three times the other. Find the numbers.

Solution: let the two numbers be x and y.

According to question $x-y=26$ -----→(1) and $x=3y$ -----→(2)

Put equation 2 in one we get

$$3y-y=26$$

$$2y=26$$

$$\mathbf{y=13}$$

put $y=13$ in equation is 2, we get $x=3 \times 13$

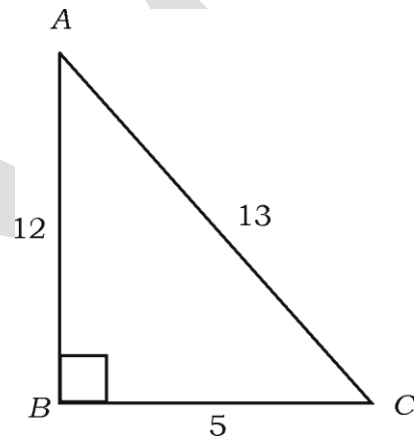
$$\mathbf{x=39}$$

19. In the given figure, write the value of $\sin C$ and $\cos A$.

Solution:

We know $\sin C = \frac{AB}{AC} = \frac{12}{13}$

$$\cos A = \frac{AB}{AC} = \frac{12}{13}$$



20. Write the probability of i) a sure event ii) an impossible event

Solution: i) a sure event is always 1

ii) an impossible event is 0

21. Find the distance between the points (5, 6) and (1, 3) using distance formula.

Solution: given points are (5, 6) and (1, 3)

$$(x_1, y_1) \text{ and } (x_2, y_2)$$

By distance formula

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1 - 5)^2 + (3 - 6)^2}$$

$$= \sqrt{16 + 9}$$

$$= \sqrt{25} = 5 \text{ units}$$

22. A fair coin is tossed twice. Find the probability of getting at least one head.

Solution: when a fair coin is tossed twice, the possible outcomes is $\{HH, HT, TH, TT\} = 4$

At least one head = {HH, HT, TH, } = 3

So probability is $P(E) = \frac{3}{4}$

23. Solve the quadratic equation $x^2+3x+2=0$ by the method of factorisation.

Solution: Given equation is $x^2+3x+2=0$. Factors of 2 is 1 and 2

$$\begin{aligned} x^2+3x+2 &= 0 \\ x^2+x+2x+2 &= 0 \\ x(x+1)+2(x+1) &= 0 \\ (x+1) &= 0 \text{ or } x+2=0 \\ x &= -1 \text{ or } x=-2 \end{aligned}$$

OR

Find the value of k for which the quadratic equation $2x^2+kx+3=0$ has real equal roots.

Solution: we have $2x^2+kx+3=0$

If the nature of the roots of the equation is real and equal, then its discriminant is $\Delta=0$

$$a=2, b=k \text{ and } c=3$$

$$b^2-4ac=0$$

$$k^2-4 \times 2 \times 3=0$$

$$k^2-24=0$$

$$k=\sqrt{24}$$

$$k=2\sqrt{6}$$

24. In triangle ABC, $DE \parallel BC$, $AD=x$, $BD=x-2$, $AE=x+2$, and $CE=x-1$. Find the value of x and hence find the AD:DB.

Solution: Given $AD=x$, $BD=x-2$, $AE=x+2$, and $CE=x-1$

By Thales theorem, $\frac{AD}{DB} = \frac{AE}{EC}$

$$\frac{x}{x-2} = \frac{x+2}{x-1}$$

$$x(x-1) = (x+2)(x-2)$$

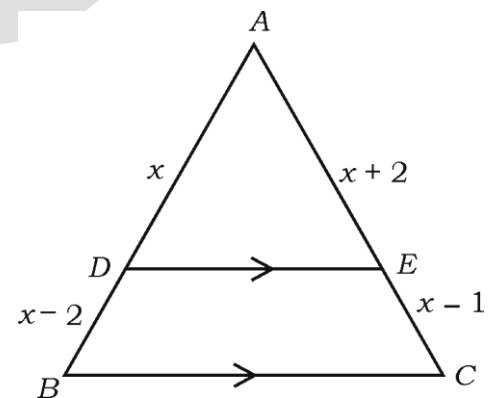
$$x^2-x = x^2-4$$

$$\mathbf{x=4}$$

then $\frac{AD}{DB}$

$$= \frac{4}{4-2} = \frac{4}{2} = \frac{2}{1}$$

Therefore AD:DB=2:1



IV. Answer the following questions

3x9=27

25. Prove that $\sqrt{3}$ is an irrational number.

Solution: Let us assume to the contrary that $\sqrt{3}$ is a rational number.

It can be expressed in the form of p/q where p and q are co-primes and $q \neq 0$.

$$\Rightarrow \sqrt{3} = p/q$$

$$\Rightarrow 3 = p^2/q^2 \text{ (Squaring on both the sides)}$$

$$\Rightarrow 3q^2 = p^2 \dots \dots \dots (1)$$

It means that 3 divides p^2 and also 3 divides p because each factor should appear two times for the square to exist.

So we have $p = 3r$

where r is some integer.

$$\Rightarrow p^2 = 9r^2 \dots\dots\dots(2)$$

from equation (1) and (2)

$$\Rightarrow 3q^2 = 9r^2$$

$$\Rightarrow q^2 = 3r^2$$

We note that the left hand side of this equation is even, while the right hand side of this equation is odd, which is a contradiction. Therefore there exists no rational number r such that $r^2=3$.

Hence the root of 3 is an irrational number.

- 26. Find the zeroes of the quadratic polynomial $p(x)=x^2+7x+10$ and verify the relationship between the zeroes and coefficients.**

Solution: we have $p(x)=x^2+7x+10$

$$x^2+7x+10$$

$$x^2+2x+5x+10$$

$$x(x+2)+5(x+2) = 0$$

$$(x+2)(x+5) = 0$$

$$x = -2 \text{ and } x = -5$$

Verification: Let first zero as α and second zero as β .

According to question,

And we know $\alpha + \beta = \frac{-b}{a}$ and $\alpha\beta = \frac{c}{a}$

$$\alpha + \beta = \frac{-(7)}{1} \text{ and } \alpha\beta = \frac{10}{1}$$

$$\alpha + \beta = -7 \quad \alpha\beta = 10$$

- 27. Calculate the mode of the following data.**

C.I	0-4	4-8	8-12	12-16	16-20	20-24
f	7	3	7	10	1	2

Solution:

C.I	f	
0-4	7	
4-8	3	
8-12	7	f_0
12-16	10	f_1
16-20	1	f_2
20-24	2	

$l=12$ and $h=4$, then by formula

$$\text{Mode} = l + \left\{ \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right\} xh.$$

$$= 12 + \left\{ \frac{10 - 7}{2 \times 10 - 7 - 1} \right\} \times 4.$$

$$= 12 + \frac{3}{20 - 7 - 1} \times 4$$

$$\begin{aligned}
 &= 12 + \frac{3}{12} \times 4 \\
 &= 12 + \frac{12}{12} \\
 &= 12 + 1 \\
 &= 13
 \end{aligned}$$

Mode= 13

OR

Calculate the median for the grouped data.

Class interval	Frequency
0-10	2
10-20	4
20-30	8
30-40	5
40-50	1
	N=20

Solution:

We have

C.I	f	cf
0-10	2	2
10-20	4	6
20-30	8	14
30-40	5	19
40-50	1	20
	N=20	

$$n/2=10, f=8, cf=6 \text{ and } h=10$$

$$\text{Median} = l + \left\{ \frac{\frac{n}{2} - fc}{f} \right\} \times h$$

$$\begin{aligned}
 \text{Median} &= 20 + \left\{ \frac{10 - 14}{8} \right\} \times 10 \\
 &= 20 + \frac{4}{8} \times 20 \\
 &= 20 + 5
 \end{aligned}$$

Median = 25

28. Prove that $\sqrt{\frac{1-\cos A}{1+\cos A}} + \sqrt{\frac{1+\cos A}{1-\cos A}} = 2\sec A$

Solution: we have

$$\begin{aligned}
 &\sqrt{\frac{1-\cos A}{1+\cos A}} + \sqrt{\frac{1+\cos A}{1-\cos A}} \\
 &= \sqrt{\frac{1-\cos A}{1+\cos A}} \times \frac{1-\cos A}{1-\cos A} + \sqrt{\frac{1+\cos A}{1-\cos A}} \times \frac{1+\cos A}{1+\cos A} \\
 &= \sqrt{\frac{(1-\cos A)^2}{1-\cos^2 A}} + \sqrt{\frac{(1+\cos A)^2}{1-\cos^2 A}} \\
 &= \frac{1-\cos A}{\sin A} + \frac{1+\cos A}{\sin A} \\
 &= \frac{1+1}{\sin A} = 2\sec A \text{ Hence the proof}
 \end{aligned}$$

OR

Prove that $\frac{1}{\sec A - 1} + \frac{1}{\sec A + 1} = 2 \operatorname{cosec} A \cdot \cot A$

Solution: we have LHS $\frac{1}{\sec A - 1} + \frac{1}{\sec A + 1}$

$$= \frac{1}{\frac{1}{\cos A} - 1} + \frac{1}{\frac{1}{\cos A} + 1}$$

$$= \frac{\cos A}{1 - \cos A} + \frac{\cos A}{1 + \cos A}$$

$$= \frac{1 - \cos A}{\cos A + \cos A} + \frac{1 + \cos A}{1 + \cos A}$$

$$= \frac{1 - \cos^2 A}{2 \cos A}$$

$$= \frac{2 \cos A}{\sin^2 A} \text{ ----- } > (1)$$

RHS $2 \operatorname{cosec} A \cdot \cot A$

$$= 2 \frac{1}{\sin A} \times \frac{\cos A}{\sin A}$$

$$= \frac{2 \cos A}{\sin^2 A} \text{ ----- } \rightarrow (2)$$

LHS = RHS

29. The length of the minute hand of a clock is 14cm, find the area swept by the minute hand in 10 minutes.

Solution: Given, We know that in 1 hour (i.e., 60 minutes), the minute hand rotates 360°

In 10 minutes, minute hand will rotate

$$= \frac{360}{60} \times 10 = 60^\circ$$

Therefore, the area swept by the minute hand in 10 minutes will be the area of a sector of 60° in a circle of 14 cm radius.

$$\text{Area of sector of angle } \theta = \frac{\theta}{360^\circ} \times \pi r^2$$

$$\text{Area of sector of } 60^\circ = \frac{60}{360^\circ} \times \frac{22}{7} \times 14 \times 14$$

$$= \frac{308}{3} \text{ cm}^2 = 102.66 \text{ cm}^2$$

Therefore, the area swept by the minute hand in 10 minutes is 102.66 cm^2

OR

Find the area of the quadrant of a circle of radius 20cm, and also find the perimeter of quadrant.

Solution: Given $r=20\text{cm}$, we have to find area of a quadrant of circle.

$$= \frac{\pi r^2}{4} = \frac{22}{7} \times \frac{20^2}{4}$$

$$= 314.2 \text{ sq cm.}$$

Now we have to find perimeter of a quadrant of a circle.

Here $\Theta=90$, $r=20$

$$\begin{aligned} \text{Length of the arc of a circle} &= \frac{\theta}{360} \times 2\pi r \\ &= \frac{90}{360} \times 2 \times \frac{22}{7} \times 20 \\ &= 31.42 \text{cm} \end{aligned}$$

30. In the given figure, find the ratio in which the point P divides the line segment AB using formula.

Solution: in the graph, point A(0, 6), point B(3, 0) and point P(2, 2)

By section formula, while taking midpoint of the line then ratio becomes m:n

$$(x, y) = \left[\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right]$$

$$(2, 2) = \left[\frac{m(3) + n(0)}{m+n}, \frac{m(0) + n(6)}{m+n} \right]$$

$$(2, 2) = \left[\frac{3m}{m+n}, \frac{6n}{m+n} \right]$$

$$2 = \frac{3m}{m+n} \quad \text{and} \quad 2 = \frac{6n}{m+n}$$

$$3m = 2m + 2n \quad \text{and} \quad 2m + 2n = 6n$$

By comparing above two equations $3m = 6n$

$$m = 2n$$

$$\frac{m}{n} = \frac{2}{1}$$

hence the ratio is 2:1

OR

Find the coordinates of the point which divides the line segment AB given in the figure internally in the ratio 1:2 using section formula.

Solution:

In the given graph, coordinates of A(2, 5) and

Coordinates of B(5, 2) in the ratio 1:2

By section formula

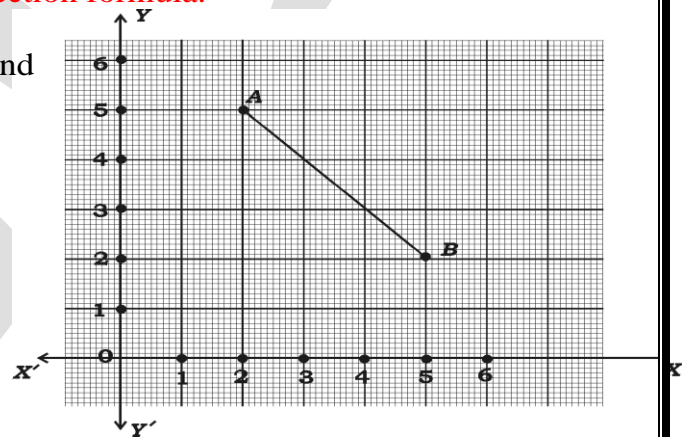
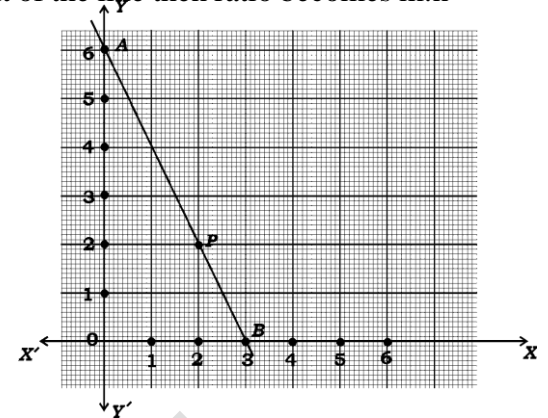
$$(x, y) = \left[\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right]$$

$$(x, y) = \left[\frac{1(5) + 2(2)}{1+2}, \frac{1(2) + 2(5)}{1+2} \right]$$

$$= \left[\frac{5+4}{3}, \frac{2+10}{3} \right]$$

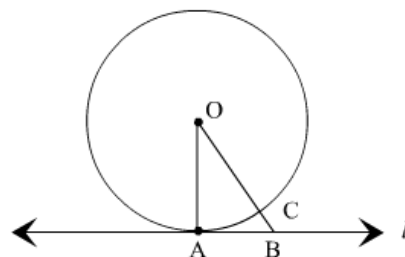
$$= \left[\frac{9}{3}, \frac{12}{3} \right]$$

$$= [3, 4]$$



31. Prove that “the tangent at any point of a circle is perpendicular to the radius through the point of contact”.

Solution:



Given: a circle C(0, r) and a tangent l at point A.

To prove: $OA \perp l$

Construction: Take a point B, other than A, on the tangent l.
join OB. Suppose OB meets the circle in C.

Proof: In figure

$OA=OC$ (Radius of the same circle)

Now, $OB=OC+BC$.

$\therefore OB > OC$

$\Rightarrow OB > OA$

$\Rightarrow OA < OB$

Thus, OA is shorter than any other line segment joining O to any point on l. Here $OA \perp l$.

- 32.** A student bought some books for Rs. 60. Had he bought 5 more books for the same amount each book would have cost Re. 1 less. Then find the number of books bought by him.

Solution: Let the number of books be = x.

Total cost of the books = Rs. 60.

\therefore Cost of each book = Rs. $\frac{60}{x}$

If the number of books is (x + 5), then the cost of each book = Rs. $\frac{60}{x+5}$

Difference in cost is one rupee = Cost of each book when number of books is (x) -

Cost of each book when number of books is (x + 5)

$$\frac{60}{x} - \frac{60}{x+5} = 1$$

$$\frac{60(x+5) - 60x}{x(x+5)} = 1$$

$$60x + 300 - 60x = x^2 + 5x$$

$$x^2 + 5x = 300$$

$$x^2 + 5x - 300 = 0$$

$$x^2 + 20x - 15x - 300 = 0$$

$$x(x+20) - 15(x+20) = 0$$

$$(x+20)(x-15) = 0$$

$$x+20=0 \text{ or } x-15=0$$

$$\therefore x = -20 \text{ or } x = 15$$

\therefore Number of books = x = 15

Number of books cannot be negative. Hence, -20 is rejected.

$$\text{Cost of books} = \frac{60}{x} = \frac{60}{15} = \text{Rs. 4}$$

- 33.** In the figure A, B and C are the points on OP, OQ and OC respectively. If $AB \parallel PQ$ and $AC \parallel PR$, then show that $BC \parallel QR$.

Solution:

In $\triangle OPQ$, we have

$AB \parallel PQ$

Therefore, by using basic proportionality theorem, we have

$$\frac{OA}{AP} = \frac{OB}{BQ} \dots \dots \dots (i)$$

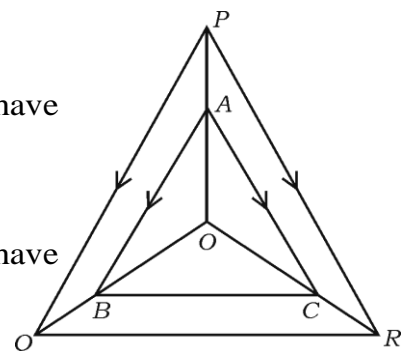
In $\triangle OPR$, we have

$AC \parallel PR$

Therefore, by using basic proportionality theorem, we have

$$\frac{OC}{CR} = \frac{OA}{AP} \dots \dots \dots (ii)$$

Comparing (i) & (ii), we get



$$OB/BQ=OC/CR$$

Therefore, by using converse of basic proportionality theorem, we get
 $BC \parallel QR$

V. Answer the following questions

4x4=16

- 34.** The 8th term of an arithmetic progression is half of its 2nd term and 11th term of this progression exceeds one third of its fourth term by 1. Find the 15th term of this progression.

Solution:

$$\text{Given that } a_8 = \frac{1}{2} a_2 \quad \text{and } a_{11} = 1 + \frac{1}{3} a_4$$

$$a+7d = \frac{1}{2}(a+d) \quad \text{and } a+10d = 1 + \frac{1}{3}(a+3d)$$

$$2a+14d = a+d \quad \text{and } 3a+30d = 3+a+3d$$

$$a+13d=0 \quad \text{and } 2a+27d=3$$

$$a=-13d \quad \text{and } 2a+27d=3$$

put $a=-13d$ in the above 2nd equation we get $2(-13d)+27d=3$

$$-26d+27d=3$$

$$d=3$$

then $a=-39$

$$\begin{aligned} \text{its 15}^{\text{th}} \text{ term is } a+14d &= -39+14 \times 3 \\ &= -39+42 \\ &= 3 \end{aligned}$$

OR

An arithmetic progression consists of 37 terms. If the sum of its middle three terms is 225 and sum of its last three terms is 429. Then find the A.P.

Solution: we have 37 terms,

The middle term is $\frac{37+1}{2} = 19^{\text{th}}$ term

Its preceding term is 18th term and its succeeding term is 20th term.

Let a, d and n be the first term, common difference and the no. of terms of given AP.

Here $n=37$

so middle most term is $n+12 \Rightarrow 37+12 \Rightarrow 18^{\text{th}}$

\therefore three middle most terms are 18th, 19th, 20th

$$a_{18}+a_{19}+a_{20}=225 \Rightarrow a+17d+a+18d+a+19d=225$$

$$\Rightarrow 3a+54d=225 \dots(1)$$

last three terms are 35th, 36th, 37th

$$a+34d+a+35d+a+36d=429$$

$$\Rightarrow 3a+105d=429 \dots(2)$$

subtracting (1) from (2), we get

$$51d=204$$

$$\Rightarrow d=4$$

putting d in (1), we get

$$3a+54 \times 4=225$$

$$3a=225-216 \Rightarrow a=3$$

Therefore the AP is $a, a+d, a+2d, a+3d, \dots$

i.e 3, 7, 11, 15,

35. Find the solution of the pair of linear equations by graphical method.

$2x+y=6$ and $x+y=4$

Solution:

We have $2x+y=6$

For this we should have to find some solutions

If $x=0$, then $y=6$, and $y=0$, then $x=3$

Similarly for $x+y=4$, if $x=0$, then $y=4$, if $y=0$ then $x=4$.

Tables are

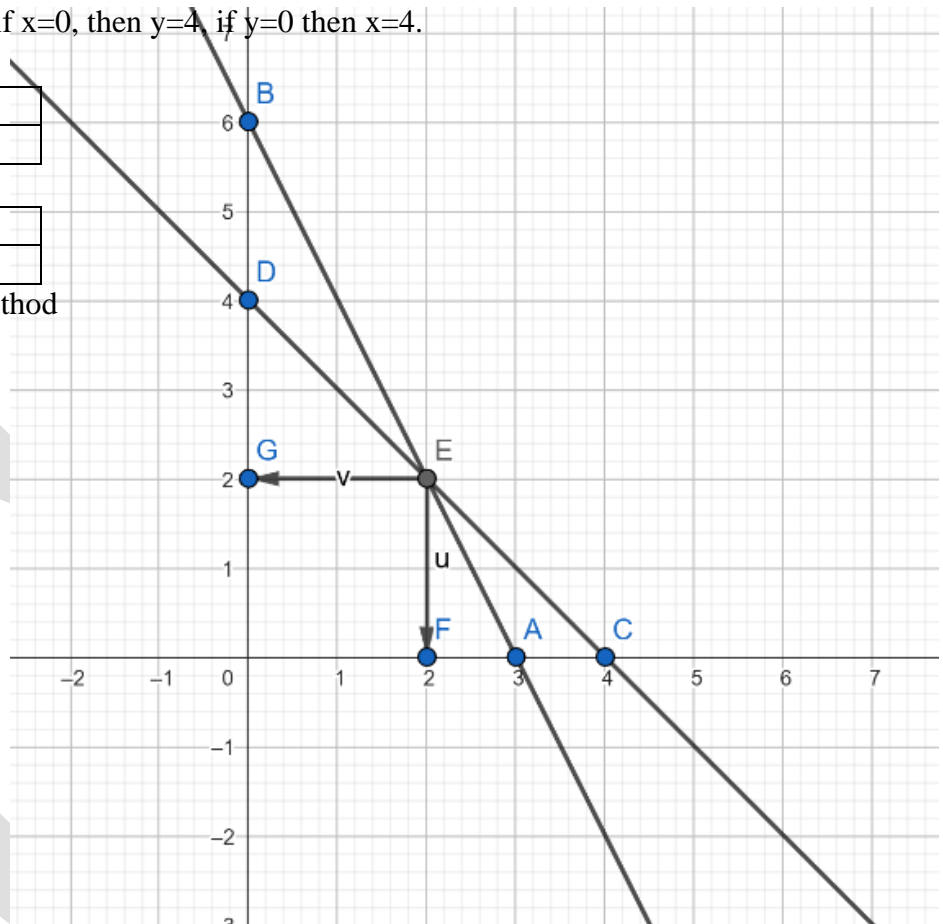
x	0	3
y	6	0

And

x	0	4
y	4	0

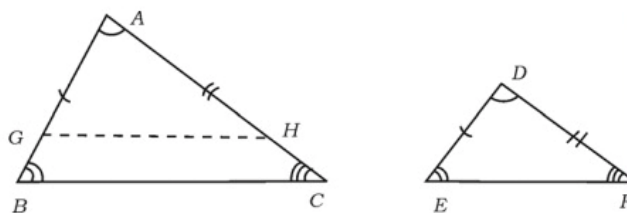
Then by graphical method

$x=2$ and $y=2$



36. Prove that "If one angle of a triangle is equal to one angle of the other triangle and the sides including these angles are proportional then prove that the two triangles are similar".

Solution:



Given: $\angle BAC = \angle EDF$

$$\angle ABC = \angle DEF$$

To prove: $\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$

Construction: Mark points G and H on the side AB and AC such that AG=DE , AH=DF

proof: in triangle AGH and DEF

AG=DE.....by construction

AH=DF by construction

$\angle GAH = \angle EDF$...Given

therefore ,

$\triangle AGH \cong \triangle FED$ by SAS congruency thus

$\angle AGH = \angle DEF$ by CPCT

but

$$\angle ABC = \angle DEF$$

$$\angle AGH = \angle ABC$$

thus

$$GH \parallel BC$$

Now , In triangle ABC

$$\frac{AB}{AG} = \frac{BC}{GH} = \frac{CA}{HA}$$

Hence ,

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$$

hence proved .

- 37.** A rope is tied from the tip of a vertical pole of length 37 m to a peg on a level ground. Another rope is tied to the same pole little below from its tip to a peg on the ground opposite to it as shown in the figure. Each rope is making an angle 30° with the ground. If the difference of the lengths of the ropes is 8 m, then find the height of the pole at which the shorter rope is tied. Also find the lengths of the ropes.

Solution: AM is the vertical pole of height 37m.

Let PA be the length of the rope = X meter.

BQ be the length of the rope = (X-8) meter

The difference of the lengths of the two ropes

$$AP - BQ = 8 \text{ m.}$$

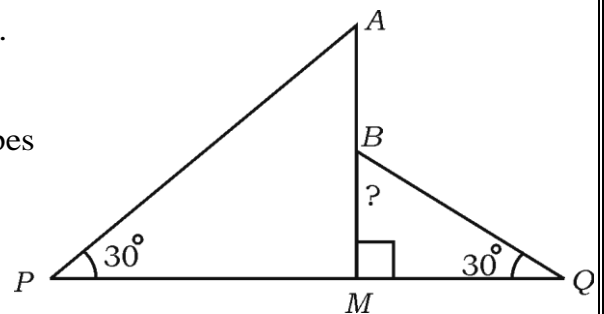
$$X - BQ = 8$$

$$X - 8 = BQ$$

In triangle PAM, $\sin \theta = \frac{AM}{AP}$

$$\sin 30 = \frac{37}{X}$$

$$\frac{1}{2} = \frac{37}{X}$$



$$X=74\text{m}$$

Then $AP-BQ=8\text{m}$

$$74-BQ=8$$

$$BQ=74-8$$

$$BQ=66\text{m}$$

In triangle MBQ $\sin\theta = \frac{BM}{BQ}$

$$\sin 30 = \frac{BM}{66}$$

$$\frac{1}{2} = \frac{BM}{66}$$

$$BM=33\text{m}$$

Then height of the pole at which the shorter rope is tied = 33m

∴ The lengths of the two ropes are 74m and 66m respectively.

- 38.** The tent of a circus company is built by canvas cloth such that a cone is surmounted on the cylindrical shape. If the height of the cylindrical shape is 9 m, the diameter of the base of the tent is 30 m and the total height of the tent is 17 m, then find the —

- a) Area of the ground occupied by the tent
b) Area of the canvas cloth used for building the tent.

Solution:

Given, **For cylinder** $d=30$, $r=15\text{m}$ and $H=9\text{m}$

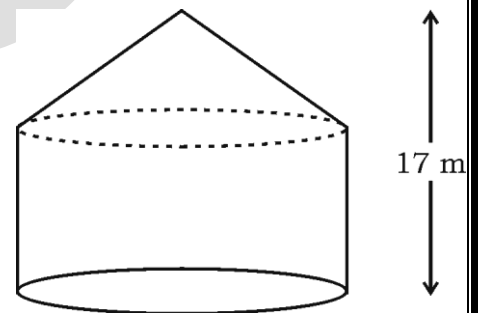
For cone, $r=15\text{m}$ (same as cylinder), height $h=17-9 = 8\text{m}$

Now we have to find slant height of cone

$$\begin{aligned} l &= \sqrt{h^2 + r^2} \\ &= \sqrt{8^2 + 15^2} \\ &= \sqrt{64 + 225} \\ &= \sqrt{289} \\ l &= 17\text{m} \end{aligned}$$

- a) Area of the ground occupied by tent = πr^2 .
= $\frac{22}{7} \times 15 \times 15$
= 707.14 sq cm
- b) Area of the canvas cloth used for building the tent.

$$\begin{aligned} &= \text{C.S.A of cylinder} + \text{C.S.A of cone} \\ &= 2\pi rH + \pi r l \\ &= \pi r(2H+l) \\ &= \frac{22}{7} \times 15 (2 \times 9 + 17) \\ &= \frac{330}{7} (18+17) \\ &= \frac{330}{7} (35) \\ &= 330 \times 5 \\ &= 1650 \text{ sq cm.} \end{aligned}$$



Note: This key answers not by board, its prepared by me.

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