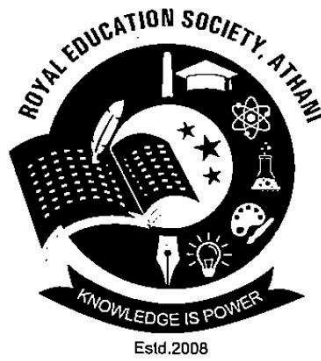


# ROYAL EDUCATION SOCIETY'S SCHOOL ATHANI



## 10<sup>th</sup> MATHEMATICS PASSING PACKAGE 2020-21



**PRACTICE  
MAKES  
PERFECT**



**EX) Solve x and y by any method.**

**$x + 2y = 3$  and  $x - 15y = 2$ .**

**Solution: Elimination Method.**

$$x + 2y = 3 \text{ ----- (1)}$$

$$7x - 15y = 2 \text{ ----- (2)}$$

$$\cancel{7x} + 14y = 21$$

$$\cancel{7x} - 15y = 2$$

$$\hline 29y = 19$$

$$y = 19/29$$

Put  $y = 19/29$  in equation (1). We get

$$x + 2y = 3$$

$$x + 2\left(\frac{19}{29}\right) = 3$$

$$x + 38/29 = 3$$

$$x = 3 - 38/29$$

$$x = 49/29$$

**EX) Solve x and y by any method.**

**$x + 3y = 6$  and  $2x - 3y = 12$**

**Solution: Elimination Method.**

$$x + 3y = 6 \text{ ----- (1)}$$

$$2x - 3y = 12 \text{ ----- (2)}$$

$$\cancel{2x} + 6y = \cancel{12}$$

$$\cancel{2x} - 3y = \cancel{12}$$

$$\begin{array}{r} - \quad + \quad - \\ \hline \end{array}$$

$$9y = 0$$

$$y = 0$$

Put  $y = 0$  in equation (1). We get

$$x + 3y = 6$$

$$x + 3(0) = 6$$

$$x + 0 = 6$$

$$x = 6$$

**EX) Solve x and y by any method.**

**$2x + y = 5$  and  $3x + 2y = 8$ .**

**Solution: Elimination Method**

$$2x + y = 5 \text{ ----- (1)}$$

$$3x + 2y = 8 \text{ ----- (2)}$$

$$\cancel{6x} + 3y = 15$$

$$\cancel{6x} + 4y = 16$$

$$\hline -y = -1$$

$$y = 1$$

Put  $y = 1$  in equation (1).

$$2x + y = 5$$

$$2x + 1 = 5$$

$$2x = 5 - 1$$

$$2x = 4$$

$$x = 2$$

**Exercise:**

EX) Solve for x & y any method.

**1)  $2x + 3y = -13$  and  $5x - 4y = -2$ .**

**2)  $5x + y = 2$  and  $6x - 3y = 1$ .**

**3)  $2x + y = 5$  and  $3x + 2y = 8$ .**

**4)  $8x + 5y = 9$  and  $3x + 2y = 4$**

**5)  $0.2x + 0.3y = 1.3$  and  $0.4x + 0.5y = 2.3$**

**6)  $2x + 3y = 11$  and  $2x - 4y = -24$ .**

**7)  $x + 2y = 3$  and  $7x - 15y = 2$ .**

**8)  $3x + 2y = 12$  and  $x - y = -1$ .**

**9)  $x + 2y = 5$  and  $-3x - 6y + 1 = 0$ .**

**10.)  $2x + y = 5$  and  $3x - 2y - 12 = 0$ .**

**1. Solve by formula method.**

$$2x^2 - 3x + 1 = 0$$

$$\text{Solution: } 2x^2 - 3x + 1 = 0$$

$$a = 2 \quad b = -3 \quad c = 1$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \times 2 \times 1}}{2 \times 2}$$

$$x = \frac{3 \pm \sqrt{9 - 8}}{4}$$

$$x = \frac{3 \pm \sqrt{1}}{4}$$

$$x = \frac{3 \pm 1}{4}$$

$$x = \frac{3+1}{4} \text{ or } x = \frac{3-1}{4}$$

$$x = 1 \text{ or } x = \frac{1}{2}$$

$$x = \frac{7+1}{2} \text{ or } x = \frac{7-1}{2}$$

$$x = 4$$

Or

$$x = 3$$

**EX) Solve by formula method**

$$x^2 - 2x - 4 = 0$$

$$\text{Solution: } a = 1 \quad b = -2 \quad c = -4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4 \times 1 \times (-4)}}{2 \times 1}$$

$$x = \frac{2 \pm \sqrt{4 + 16}}{2}$$

$$x = \frac{2 \pm \sqrt{20}}{2}$$

$$x = \frac{2 \pm 2\sqrt{5}}{2}$$

$$x = \frac{2(1 \pm \sqrt{5})}{2}$$

$$x = 1 + \sqrt{5}$$

$$x = 1 - \sqrt{5}$$

**2) Solve by formula method.**

$$x^2 - 7x + 12 = 0$$

$$\text{Solution: } x^2 - 7x + 12 = 0$$

$$a = 1 \quad b = -7 \quad c = 12$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4 \times 1 \times 12}}{2 \times 1}$$

$$x = \frac{7 \pm \sqrt{49 - 48}}{2}$$

$$x = \frac{7 \pm \sqrt{1}}{2}$$

$$x = \frac{7 \pm 1}{2}$$

**Exercise: solve by formula method.**

$$1. x^2 - 3x - 10 = 0$$

$$2. x^2 + 7x - 60 = 0$$

$$3. 3x^2 - 5x + 2 = 0$$

$$4. 2x^2 - 3x + 1 = 0$$

$$5. 3x^2 - 12x + 15 = 0$$

$$6. x^2 + 2x - 3 = 0$$

$$7. x^2 - 2x - 3 = 0$$

$$8. 3x^2 + 5x - 2 = 0$$

$$9. 3x^2 - 2\sqrt{6}x + 2 = 0$$

$$10. \sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$$

**1) Prove that  $3 + \sqrt{5}$  is irrational number.**

**Solution:** let us assume that  $3 + \sqrt{5}$  is rational number.

$$3 + \sqrt{5} = \frac{p}{q} \quad p \in \mathbb{Z} \text{ and } q \neq 0.$$

$$\sqrt{5} = \frac{p}{q} - 3$$

$$\sqrt{5} = \frac{p-3q}{q}$$

w.k.t  $\frac{p-3q}{q}$  is rational number.

$\sqrt{5}$  is a irrational number.

$\therefore 3 + \sqrt{5}$  Is irrational number.

**2) Prove that  $3 - \sqrt{5}$  is irrational number.**

**Solution:** let us assume that  $3 - \sqrt{5}$  is rational number.

$$3 - \sqrt{5} = \frac{p}{q} \quad p \in \mathbb{Z} \text{ and } q \neq 0.$$

$$-\sqrt{5} = \frac{p}{q} - 3$$

$$-\sqrt{5} = \frac{p-3q}{q}$$

$$\sqrt{5} = \frac{-p+3q}{q}$$

w.k.t  $\frac{-p+3q}{q}$  is rational number.

$\sqrt{5}$  is a irrational number.

$\therefore 3 - \sqrt{5}$  Is irrational number.

**3) Prove that  $3 + 2\sqrt{5}$  is irrational number.**

**Solution:** : let us assume that  $3 + 2\sqrt{5}$  is rational number.

$$3 + 2\sqrt{5} = \frac{p}{q} \quad p \in \mathbb{Z} \text{ and } q \neq 0.$$

$$2\sqrt{5} = \frac{p}{q} - 3$$

$$2\sqrt{5} = \frac{p-3q}{q}$$

$$\sqrt{5} = \frac{p-3q}{2q}$$

w.k.t  $\frac{p-3q}{2q}$  is rational number.

$\sqrt{5}$  is a irrational number.

$\therefore 3 + 2\sqrt{5}$  Is irrational number.

**Exercise**

**Prove that following numbers are irrational number.**

1)  $5 + \sqrt{3}$

2)  $5 - \sqrt{3}$

3)  $2 + \sqrt{3}$

4)  $2 + \sqrt{5}$

5)  $3 + 5\sqrt{2}$

6)  $6 + \sqrt{2}$

7)  $3 - \sqrt{7}$

8)  $5 - \sqrt{5}$

9)  $3 + \sqrt{7}$

10)  $2 - \sqrt{5}$

• **DISTANCE FORMULA:**

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

**Ex) Find the distance between two points (6, 5) and (4, 4).**

**Solution:**  $(6, 5) = (x_1, y_1)$

$$(4, 4) = (x_2, y_2)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(4 - 6)^2 + (4 - 5)^2}$$

$$d = \sqrt{(-2)^2 + (-1)^2}$$

$$d = \sqrt{4 + 1}$$

$$d = \sqrt{5} \text{ units.}$$

**Ex2) Find the distance between two points (4, 7) and (2, 3).**

**Solution:**  $(4, 7) = (x_1, y_1)$

$$(2, 3) = (x_2, y_2)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(2 - 4)^2 + (3 - 7)^2}$$

$$d = \sqrt{(-2)^2 + (-4)^2}$$

$$d = \sqrt{4 + 16}$$

$$d = \sqrt{20}$$

$$d = 2\sqrt{5} \text{ Units.}$$

**EX3) Find the distance between two points (2, 3) and (6,-8).by using formula.**

**Solution:**  $(2, 3) = (x_1, y_1)$

$$(6, -8) = (x_2, y_2)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(6 - 2)^2 + (-8 - 3)^2}$$

$$d = \sqrt{(4)^2 + (-11)^2}$$

$$d = \sqrt{16 + 121}$$

$$d = \sqrt{137} \text{ units.}$$

**Exercise**

**Find the distance between following points.**

- 1) Find the distance between two points (-2, 5) and (-5, 2).
- 2) Find the distance between two points (1, 7) and (-2, 3).
- 3) Find the distance between two points (-6, 4) and (5, -7).
- 4) Find the distance between two points (-4, -7) and (-2, -3).
- 5) Find the distance between two points (1, 1) and (3, 2).
- 6) Find the distance between two points (-3, 2) and (2, -3).
- 7) Find the distance between two points (4, 3) and (8, -3).

➤ **MID POINT FORMULA.**

$$P(X, Y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

**EX) find the midpoint of the points  $(-4, 1)$  and  $(5, 2)$ .**

**Solution:**  $(-4, 1) = (x_1, y_1)$

$$(5, 2) = (x_2, y_2)$$

$$P(X, Y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$P(X, Y) = \left( \frac{-4 + 5}{2}, \frac{1 + 2}{2} \right)$$

$$P(X, Y) = \left( \frac{1}{2}, \frac{3}{2} \right)$$

**EX) find the midpoint of the points  $(3, 1)$  and  $(4, 5)$ .**

**Solution:**  $(3, 1) = (x_1, y_1)$

$$(4, 5) = (x_2, y_2)$$

$$P(X, Y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$P(X, Y) = \left( \frac{3 + 4}{2}, \frac{1 + 5}{2} \right)$$

$$P(X, Y) = \left( \frac{7}{2}, \frac{6}{2} \right)$$

$$P(X, Y) = \left( \frac{7}{2}, 3 \right)$$

**EX) find the midpoint of the points  $(5, 3)$  and  $(5, 1)$ .**

**Solution:**  $(5, 3) = (x_1, y_1)$

$$(5, 1) = (x_2, y_2)$$

$$P(X, Y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$P(X, Y) = \left( \frac{5 + 5}{2}, \frac{3 + 1}{2} \right)$$

$$P(X, Y) = \left( \frac{10}{2}, \frac{4}{2} \right)$$

$$P(X, Y) = (5, 2)$$

➤ **SECTION FORMULA:**

$$P(X, Y) = \left( \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right)$$

**EX) Find the coordinates of the point which divides the join of  $(-1, 7)$  and  $(4, -3)$  in the ratio 2:3.**

**Solution:**  $(-1, 7) = (x_1, y_1)$

$$(4, -3) = (x_2, y_2) \quad m_1 : m_2 = 2 : 3$$

$$P(X, Y) = \left( \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right)$$

$$P(X, Y) = \left( \frac{(2)(4) + 3(-1)}{2 + 3}, \frac{(2)(-3) + 3(7)}{2 + 3} \right)$$

$$P(X, Y) = \left( \frac{8 - 3}{5}, \frac{-6 + 21}{5} \right)$$

$$P(X, Y) = (1, 3)$$

**Exercise**

**EX) Find the coordinates of the point which divides the join of  $(4, -1)$  and  $(-2, -3)$  in the ratio 1:3.**

**EX) Find the coordinates of the point which divides the join of  $(-6, 10)$  and  $(3, -8)$  in the ratio 2:7.**

**EX) Find the midpoint of the points  $(5, -6)$  and  $(-1, -4)$ .**

**EX) Find the midpoint of the points  $(2, -2)$  and  $(-7, 4)$ .**

**EX) Find the quotient and remainder when  $p(x) = 3x^3 + x^2 + 2x + 5$  is divided by  $g(x) = x^2 + 2x + 1$ .**

**Solution:**  $p(x) = 3x^3 + x^2 + 2x + 5$

$$g(x) = x^2 + 2x + 1$$

$$\begin{array}{r}
 3x - 5 \\
 x^2 + 2x + 1 \overline{) 3x^3 + x^2 + 2x + 5} \\
 \underline{3x^3 + 6x^2 + 3x} \phantom{+ 5} \\
 -5x^2 - x + 5 \\
 \underline{-5x^2 - 10x - 5} \\
 + \phantom{+} + \phantom{+} \\
 9x + 10
 \end{array}$$

**Quotient =  $3x - 5$**

**Remainder =  $9x + 10$**

**EX) Find the quotient and remainder when  $p(x) = x^3 - 3x^2 + 5x - 3$  is divided by  $g(x) = x^2 - 2$ .**

**Solution:**  $p(x) = x^3 - 3x^2 + 5x - 3$

$$g(x) = x^2 - 2$$

$$\begin{array}{r}
 x - 3 \\
 x^2 - 2 \overline{) x^3 - 3x^2 + 5x - 3} \\
 \underline{x^3 \phantom{- 3x^2} - 2x} \phantom{- 3} \\
 - \phantom{+} + \\
 -3x^2 + 7x - 3 \\
 \underline{-3x^2 \phantom{+ 7x} + 6} \\
 + \phantom{+} - \\
 7x - 9
 \end{array}$$

**Quotient =  $x - 3$**

**Remainder =  $7x - 9$**

**EX) Show that polynomial  $x^2 + 3x + 1$  is a factor of polynomial  $3x^4 + 5x^3 - 7x^2 + 2x + 2$ .**

**Solution:**  $p(x) = 3x^4 + 5x^3 - 7x^2 + 2x + 2$

$$g(x) = x^2 + 3x + 1$$

$$\begin{array}{r}
 3x^2 + 4x + 2 \\
 x^2 + 3x + 1 \overline{) 3x^4 + 5x^3 - 7x^2 + 2x + 2} \\
 \underline{3x^4 + 9x^3 - 3x^2} \phantom{+ 2x + 2} \\
 -4x^3 - 10x^2 + 2x + 2 \\
 \underline{-4x^3 - 12x^2 - 4x} \phantom{+ 2} \\
 + \phantom{+} + \phantom{+} \\
 2x^2 + 6x + 2 \\
 \underline{2x^2 + 6x + 2} \\
 - \phantom{+} - \phantom{+} \\
 0
 \end{array}$$

### Exercise

**EX) Find the quotient and remainder when  $p(x) = x^4 - 3x^2 + 4x + 5$  is divided by  $g(x) = x^2 - x + 1$ .**

**EX) Find the quotient and remainder when  $p(x) = x^3 - 3x^2 + 5x - 3$  is divided by  $g(x) = 2 - x^2$ .**

**EX) Show that polynomial  $x - 2$  is a factor of polynomial  $x^3 - 3x^2 + 3x - 2$ .**

## ➤ AREA OF SECTOR

$$\diamond \text{ Area of Sector} = \frac{\theta}{360^\circ} \times \pi r^2$$

$$\diamond \text{ Length of arc} = \frac{\theta}{360^\circ} \times 2\pi r$$

**EX) Find the area of a sector the circle with radius 6cm if angle of sector is  $60^\circ$ .**

**Solution:** Given  $r = 6\text{cm}$   $\theta = 60^\circ$

$$\begin{aligned}\text{Area of Sector} &= \frac{\theta}{360^\circ} \times \pi r^2 \\ &= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 6 \times 6 \\ &= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 6 \times 6 \\ &= \frac{22}{7} \times 6\end{aligned}$$

$$\text{Area of Sector} = \frac{136}{7} \text{ cm}^2$$

**EX) In a circle of radius 21 cm if angle, an arc subtends an angle of  $40^\circ$  at the centre. Find the length of the arc.**

**Solution:** Given  $r = 21\text{cm}$   $\theta = 40^\circ$

$$\begin{aligned}\text{Length of arc} &= \frac{\theta}{360^\circ} \times 2\pi r \\ &= \frac{40^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 21 \\ &= \frac{1}{9} \times 2 \times \frac{22}{7} \times 21\end{aligned}$$

$$\text{Length of arc} = \frac{136}{7} \text{ cm}^2$$

**EX) In a circle of radius 21 cm if angle, an arc subtends an angle of  $60^\circ$  at the centre find the area of segment.**

**Solution:** Given  $r = 21\text{cm}$   $\theta = 60^\circ$

$$\begin{aligned}\text{Area of Sector} &= \frac{\theta}{360^\circ} \times \pi r^2 \\ &= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 21 \times 21 \\ &= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 21 \times 21\end{aligned}$$

$$\text{Area of Sector} = 231 \text{ cm}^2$$

$$\begin{aligned}\text{Area of equilateral triangle} &= \frac{\sqrt{3}}{4} a^2 \\ &= \frac{\sqrt{3}}{4} \times 21 \times 21\end{aligned}$$

$$\text{Area of equilateral triangle} = 441 \frac{\sqrt{3}}{4} \text{ cm}^2$$

Area of segment = Area of sector – Area of Equilateral Triangle

$$\text{Area of Sector} = 231 - 441 \frac{\sqrt{3}}{4} \text{ cm}^2$$

## Exercise

**EX) Find the area of a sector the circle with radius 7cm if angle of sector is  $90^\circ$ .**

**EX) In a circle of radius 21 cm if angle, an arc subtends an angle of  $40^\circ$  at the centre. Find the length of the arc.**

**EX) In a circle of radius 14 cm if angle, an arc subtends an angle of  $60^\circ$  at the centre find the area of segment.**



➤ PROBABILITY:

$$P(E) = \frac{n(E)}{n(S)}$$

**Ex) A die is thrown once, Find the probability of getting A) A prime number B) a number lying between 2 and 6. C) An odd number. D) an perfect square.**

**Solution:** A die is thrown once,

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$n(S) = 6$$

**A) A prime number**

$$E = \{2, 3, 5\}, n(E) = 3$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{3}{6}$$

$$P(E) = \frac{1}{2}$$

**B) A number lying between 2 and 6.**

$$E = \{3, 4, 5\}, n(E) = 3$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{3}{6}$$

$$P(E) = \frac{1}{2}$$

**C) An odd number.**

$$E = \{1, 3, 5\}, n(E) = 3$$

$$E = \{3, 4, 5\}, n(E) = 3$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{3}{6}$$

$$P(E) = \frac{1}{2}$$

**D) A perfect square.**

$$E = \{1, 4\}, n(E) = 2$$

$$P(E) = \frac{n(E)}{n(S)}$$

$$P(E) = \frac{2}{6}$$

$$P(E) = \frac{1}{3}$$

**EX) A box contains 90 disc which are numbered from 1 to 90. If one disc is drawn at random from box, find the probability that it bears A) a two digit number B) A perfect a square number.**

**Solution:**  $n(S) = 90$

**A) a two digit number**

$$n(E) = 81$$

$$P(E) = \frac{n(E)}{n(S)} = \frac{81}{90}$$

$$P(E) = \frac{9}{10}$$

**B) A perfect a square number.**

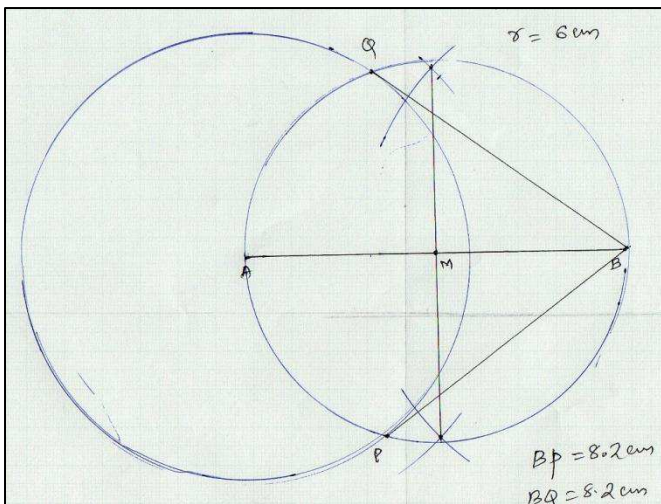
$$n(E) = 9$$

$$P(E) = \frac{n(E)}{n(S)} = \frac{9}{90} = 1/9$$

## CONSTRUCTION:

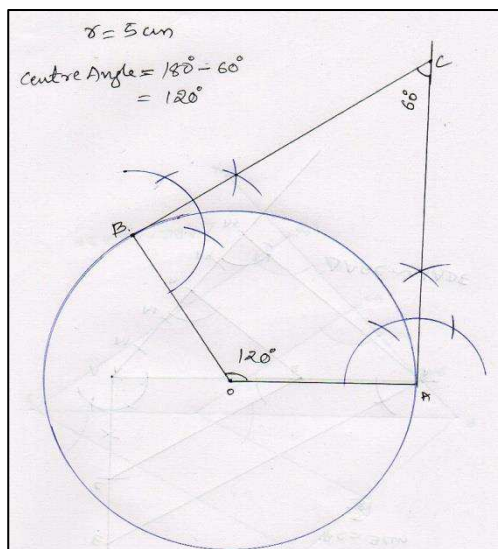
Ex) draw a circle of radius 6cm. From a point 10 cm away from its centre, construct the pair of tangents to the circle and measure their lengths.

**Solution:**



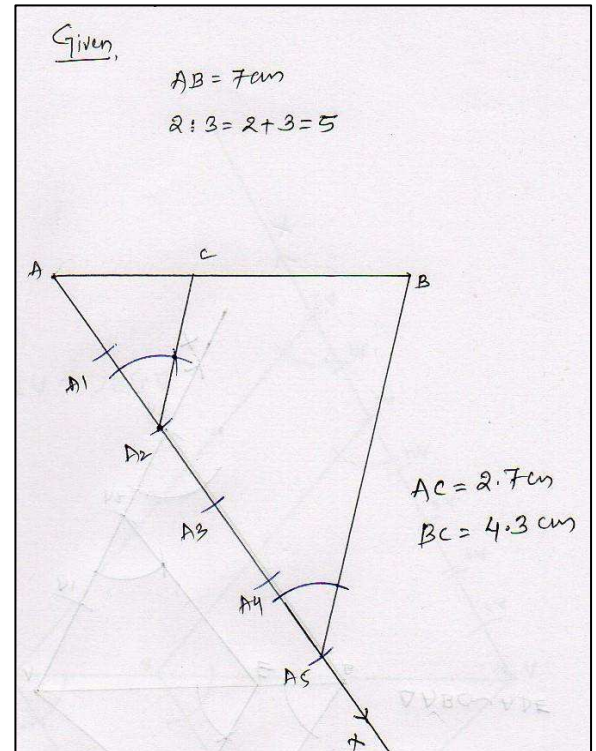
EX) Draw a pair of tangents to a circle of radius 5cm which are inclined to each other at an angle of  $60^\circ$ .

**Solution:**



**EX)** Draw a line segment of length of 7cm and divided in the 2:3. Measure the two parts.

**Solution:**



## **Exercise**

1) Draw a circle of radius 4.5cm. From a point 11 cm away from its centre, construct the pair of tangents to the circle and measure their lengths.

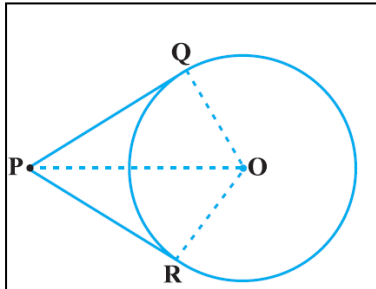
2) Draw a pair of tangents to a circle of radius 5.6cm which are inclined to each other at an angle of  $70^\circ$ .

2) Draw a line segment of length of 7cm and divided in the 2:3. Measure the two parts.

### 3 MARKS QUESTION :

**Theorem:** The lengths of tangents drawn from an external point to a circle are equal.

**Proof:**



O is centre of circle. P is external point, PQ and PR are tangents.

To prove that  $PQ = PR$

Join OQ, OR and OP.

In  $\triangle OPQ$  and  $\triangle OPR$

$$\angle Q = \angle R = 90^\circ$$

$OQ = OR$  are radii of circle.

OP is common hypotenuse

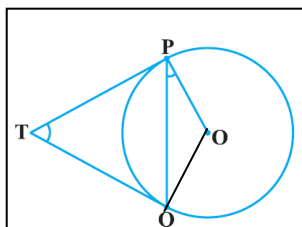
By using RHS rule.

$$\triangle OPQ \cong \triangle OPR$$

$$PQ = PR$$

**Theorem:** Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that  $\angle PTQ = 2 \angle OPQ$ .

**Proof:**



O is centre of circle. TP and TQ are two tangents.

Join OQ. We know that.  $\triangle OPQ$  is isosceles triangle.

$$2 \angle OPQ + \angle POQ = 180^\circ \text{ ----- (1)}$$

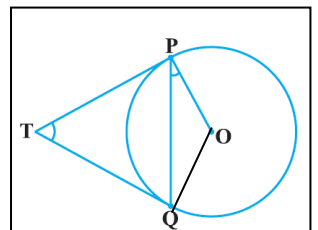
$$\angle PTQ + \angle POQ = 180^\circ \text{ ----- (1)}$$

From equation (1) and (2)

$$2 \angle OPQ + \cancel{\angle POQ} = \angle PTQ + \cancel{\angle POQ}$$

$$\angle PTQ = 2 \angle OPQ$$

**Theorem:** Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.



**Proof:** O is the centre of circle. TP and TQ are two tangents. To show that

$$\angle POQ + \angle PTQ = 180^\circ$$

We know that

$\angle Q = \angle P = 90^\circ$  (The tangent at any point of a circle is perpendicular to the radius through the point of contact).

And OPTQ is quadrilateral .

$$\angle POQ + \angle OPT + \angle PTQ + \angle OQT = 360^\circ$$

$$\angle POQ + 90^\circ + \angle PTQ + 90^\circ = 360^\circ$$

$$\angle POQ + \angle PTQ + 180^\circ = 360^\circ$$

$$\angle POQ + \angle PTQ = 360^\circ - 180^\circ$$

$$\angle POQ + \angle PTQ = 180^\circ$$



## Ogive Graph:

EX 1) Draw the less than type ogive of following distribution table.

C.I	100-120	120-140	140-160	160-180	180-200
f	12	14	8	6	10

Solution:

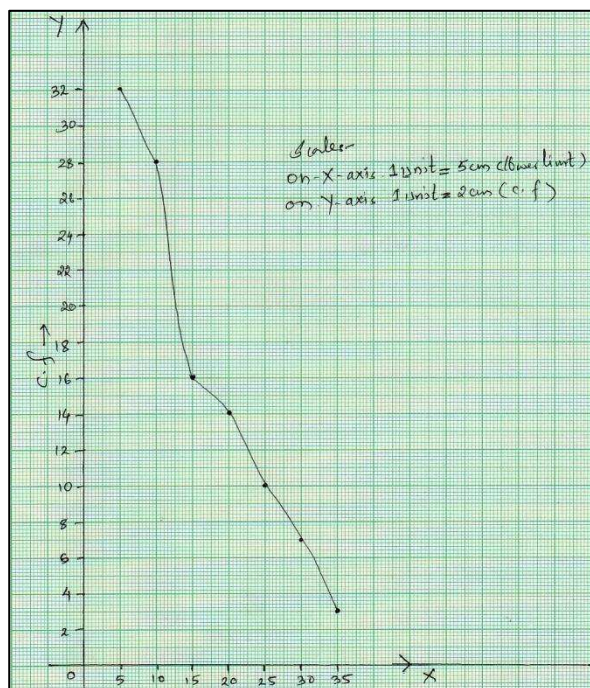
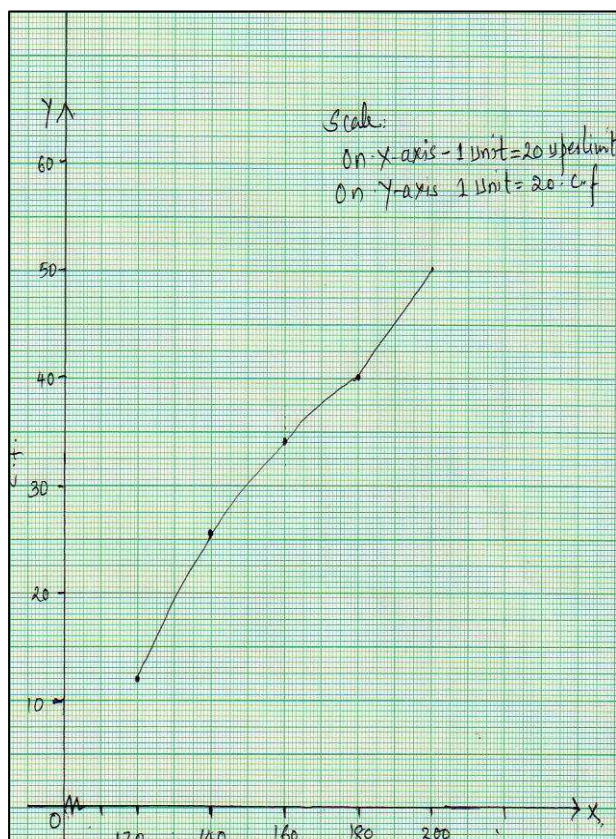
C.I	f	c.f
Less than 120	12	12
Less than 140	14	14+12=26
Less than 160	8	26+8=34
Less than 180	6	34+6=40
Less than 200	10	40+10=50
	N= 50	

2) Draw the more than type ogive of following distribution table.

C.I	5-10	10-15	15-20	20-25	25-30	30-35	35-40
f	2	12	2	4	3	4	3

Solution:

C.I	f	C.F
More than 5	2	30
More than 10	12	30-2= 28
More than 15	2	28-12= 16
More than 20	4	16-2= 14
More than 25	3	14-4= 10
More than 30	4	10-3= 7
More than 35	3	7-4= 3
	N=30	



### Mean:

$$\bar{X} = \frac{\sum fx}{\sum f}$$

Ex) find Mean of the following distribution table.

C.I	0-2	2-4	4-6	6-8	8-10	10-12	12-14
f	1	2	1	5	6	2	3

**Solution:**

C.I	f	C.M (x)	fx
0-2	1	1	1
2-4	2	3	6
4-6	1	5	5
6-8	5	7	35
8-10	6	9	54
10-12	3	11	33
12-14	2	13	26
	$\sum f = 20$		$\sum fx = 160$

$$\bar{X} = \frac{\sum fx}{\sum f} = \frac{160}{20}$$

$$\bar{X} = 8$$

**Exercise:**

Ex) find Mean of the following distribution table.

C.I	5-15	15-25	25-35	35-45	45-55	55-65
f	6	11	21	23	14	5

### Mode :

$$\text{Mode} = l + \left( \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h$$

EX) find the mode of the following data

C.I	1-3	3-5	5-7	7-9	9-11
f	7	8	2	2	1

**Solution:**

$$f_0 = 7$$

$$= l + \left( \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h$$

$$f_1 = 8$$

$$= 3 + \left( \frac{8-7}{2(8)-7-2} \right) \times 2$$

$$f_2 = 2$$

$$= 3 + \left( \frac{1}{16-7-2} \right) \times 2$$

$$l = 3$$

$$= 3 + \left( \frac{1}{7} \right) \times 2$$

$$h = 2$$

$$= 3 + \left( \frac{2}{7} \right)$$

$$= 3 + 0.285$$

$$\text{Mode} = 3.285$$

**Exercise:**

1) Find the Mode of the following data.

C.I	0-20	20-40	40-60	60-80	80-100	100-120
f	10	35	52	61	38	29

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## Median:

$$\text{Median} = l + \left( \frac{\frac{n}{2} - c.f}{f} \right) \times h$$

EX) find median of the following distribution table.

C.I	65-85	85-105	105-125	125-145	145-165	165-185	185-205
f	4	5	13	20	14	8	4

Solution:

C.I	f	c.f
65-85	4	4
85-105	5	4+5=9
105-125	13	9+13=22 c.f
125-145	f 20	22+20=42
145-165	14	42+14=56
165-185	8	56+8=64
185-205	4	64+4=68
	N=68	

Solution:

$$\text{Median} = l + \left( \frac{\frac{n}{2} - c.f}{f} \right) \times h$$

$$N = 68, N/2 = 68/2 = 34$$

$$L = 125, f = 20, c.f = 22, h = 20$$

$$\text{Median} = 125 + \left( \frac{34 - 22}{20} \right) \times 20$$

$$= 125 + \left( \frac{12}{20} \right) \times 20$$

$$= 125 + 12$$

$$\text{Median} = 137$$

## Exercise:

1) Find median of the following distribution table.

C.I	118-126	127-135	136-144	145-153	154-162	163-171	172-180
f	3	5	9	12	5	4	2

2) Find median of the following distribution table.

C.I	0-10	10-20	20-30	30-40	40-50	50-60
f	5	8	20	15	7	5

3) Find mean, Median, Mode of the following distribution table.

C.I	1-4	4-7	7-10	10-13	13-16	16-19
f	6	30	40	16	4	4

4) Draw the less than type ogive of following distribution table.

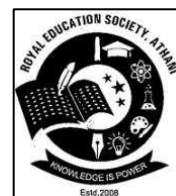
C.I	40-45	45-50	50-55	55-60	60-65	65-70	70-75
f	2	3	8	6	6	3	2

5) Draw the more than type ogive of following distribution table.

C.I	135-140	140-145	145-150	150-155	155-160	160-165
f	4	7	18	11	6	5

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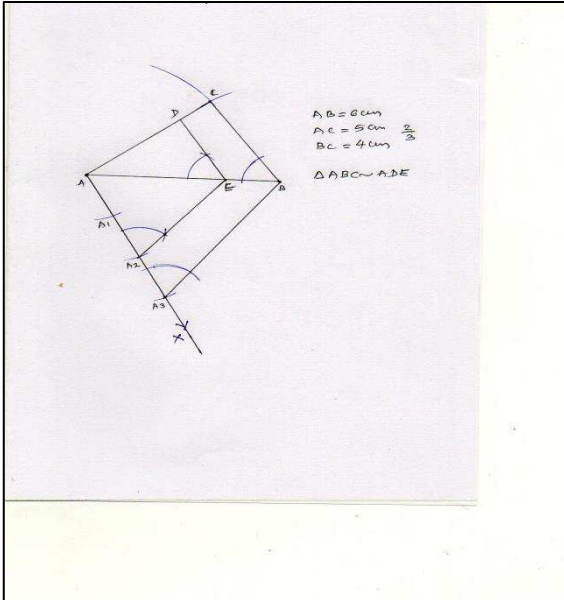
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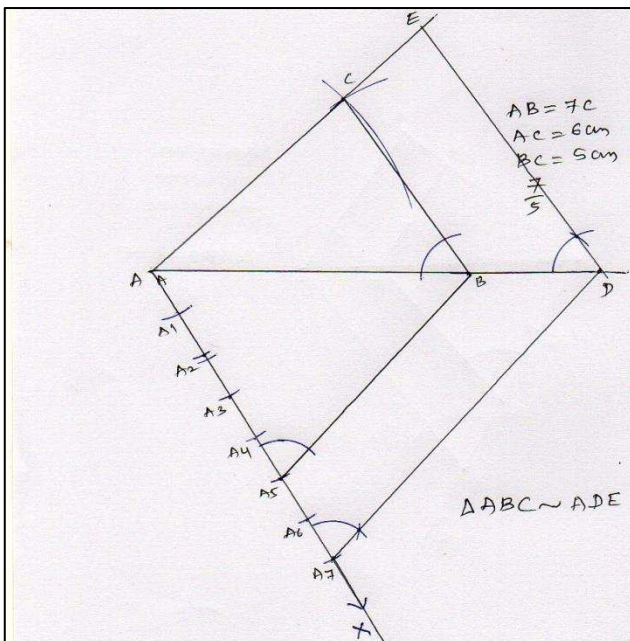


## Construction:

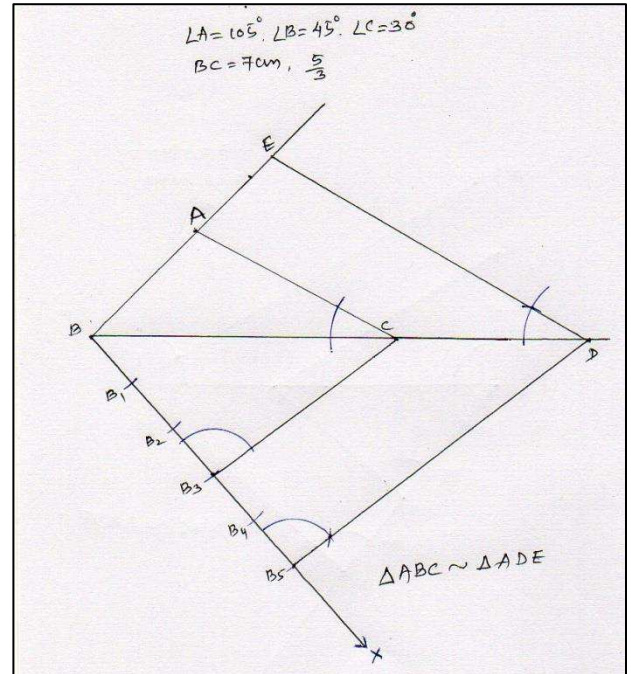
EX) Construct a triangle of sides 4cm, 5cm, and 6cm and then a triangle similar to it whose sides are  $\frac{2}{3}$  of the corresponding sides of the first triangle.



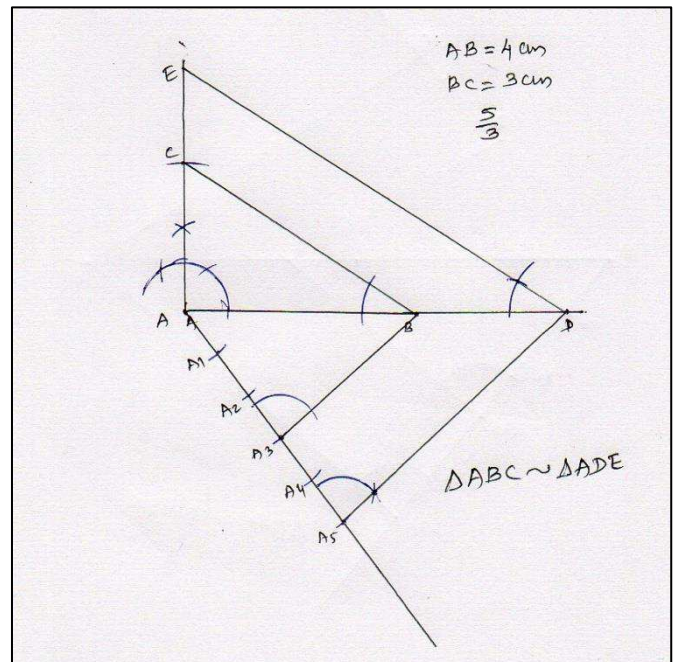
EX) Construct a triangle with sides 5cm, 6cm and 7cm and then another triangle whose sides are  $\frac{7}{5}$  of the corresponding sides of the first triangle.



EX) Draw a triangle  $ABC$  with side  $BC=7\text{cm}$ ,  $\angle B = 45^\circ$  and  $\angle A = 105^\circ$  then construct a triangle whose sides are  $\frac{4}{3}$  times the corresponding sides of the  $\Delta ABC$ .



EX) Draw a right triangle in which the sides (other than hypotenuse) are of lengths 4cm and 3cm. Then construct another triangle whose sides are  $\frac{5}{3}$  times the corresponding side of the given triangle.



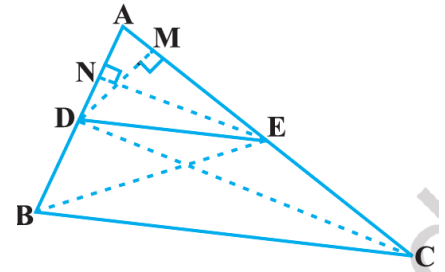
#### 4 MARKS QUESTION :

#### THALE'S THEOREM ( B P T )

**SATEMENT:** *"If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct Points, the other two sides are divided in the same ratio"*

**Proof:**  $\triangle ABC$   $DE \parallel BC$ .

To prove  $\frac{AD}{BD} = \frac{AE}{EC}$



Join BE and CD and then draw  $DM \perp AC$  and  $EN \perp AB$ .

*Area of triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$*

$$\frac{\text{Area}(\triangle ADE)}{\text{Area}(\triangle BDE)} = \frac{\frac{1}{2} \times AD \times EN}{\frac{1}{2} \times DB \times EN}$$

$$\frac{\text{Area}(\triangle ADE)}{\text{Area}(\triangle BDE)} = \frac{AD}{DB} \text{ ----- (1)}$$

$$\frac{\text{Area}(\triangle ADE)}{\text{Area}(\triangle BDE)} = \frac{\frac{1}{2} \times AD \times EN}{\frac{1}{2} \times DB \times EN}$$

$$\frac{\text{Area}(\triangle ADE)}{\text{Area}(\triangle DEC)} = \frac{\frac{1}{2} \times DM \times AE}{\frac{1}{2} \times DM \times EC}$$

$$\frac{\text{Area}(\triangle ADE)}{\text{Area}(\triangle DEC)} = \frac{AE}{EC} \text{ ----- (2)}$$

From questions (1) and (2) we get

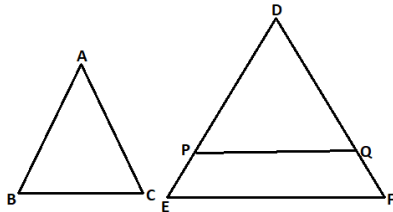
$$\frac{AD}{BD} = \frac{AE}{EC}$$



**Theorem:** A.A.A Similarity

*If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio (or proportion) and hence the two triangles are similar.*

**Proof:**



In  $\triangle ABC$  and  $\triangle DEF$

$$\angle B = \angle E \text{ And } \angle C = \angle F$$

To prove  $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$

Cut  $DP = AB$  and  $DQ = AC$  join PQ

In  $\triangle ABC$  and  $\triangle DPQ$

$$\angle A = \angle D$$

$$AB = DP$$

$$AC = DQ$$

$$\triangle ABC \cong \triangle DPQ \text{ (By SAS rule)}$$

$$\angle B = \angle P$$

$$\angle E = \angle P$$

PQ is parallel to EF, By Thales theorem.

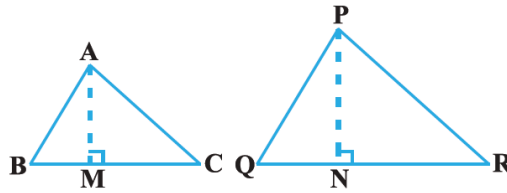
$$\frac{DP}{DE} = \frac{DQ}{DF}$$

Similarly  $\boxed{\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}}$

## Areas of Similar Triangles:

**“The ratio of the areas two similar triangle is equal to the square of the ratio of their corresponding sides”.**

**Proof:**



$\triangle ABC$  and  $\triangle PQR$  are similar triangles  $\triangle ABC \sim \triangle PQR$

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$

To prove  $\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AB^2}{PQ^2} = \frac{BC^2}{QR^2} = \frac{AC^2}{PR^2}$

Draw  $AM \perp BC$  and  $PN \perp QR$

In  $\triangle ABM$  and  $\triangle PQN$

$$\angle B = \angle Q$$

$$\angle M = \angle N = 90^\circ$$

By A.A.A similarity

$$\triangle ABM \sim \triangle PQN$$

$$\frac{AB}{PQ} = \frac{BM}{QN} = \frac{AM}{PN}$$

$$\frac{AB}{PQ} = \frac{AM}{PN} \text{ -----(1)}$$

$$\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{\frac{1}{2} \times AM \times BC}{\frac{1}{2} \times PN \times QR}$$

$$\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AM}{PN} \times \frac{BC}{QR}$$

$$\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AB}{PQ} \times \frac{BC}{QR} \quad (\text{From 1})$$

$$\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AB}{PQ} \times \frac{AB}{PQ}$$

$$\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AB^2}{PQ^2}$$

Similarly  $\frac{\text{area of } \triangle ABC}{\text{area of } \triangle PQR} = \frac{AB^2}{PQ^2} = \frac{BC^2}{QR^2} = \frac{AC^2}{PR^2}$

## Pythagoras Theorem :

**Statement:** "In a right triangle the square of the hypotenuse is equal to the sum of the squares of the other two sides."

**Proof:**  $\triangle ABC$  right triangle at  $\angle B = 90^\circ$

To prove ,  $AC^2 = AB^2 + BC^2$

Draw  $BD \perp AC$

In  $\triangle ABC$  and  $\triangle ADB$ .

$\angle B = \angle D = 90^\circ$

$\angle A$  is common

By A.A.A similarity

$\triangle ABC \sim \triangle ADB$ .

$$\frac{AB}{AD} = \frac{BC}{DB} = \frac{AC}{AB}$$

$$\frac{AB}{AD} = \frac{AC}{AB}$$

$$AB^2 = AC \times AD \text{ -----(1)}$$

Similarly  $\triangle ABC \sim \triangle BDC$ .

$\angle B = \angle D = 90^\circ$

$\angle C$  is common

By A.A.A similarity

$\triangle ABC \sim \triangle BDC$

$$\frac{AB}{BD} = \frac{BC}{DC} = \frac{AC}{BC}$$

$$\frac{BC}{DC} = \frac{AC}{BC}$$

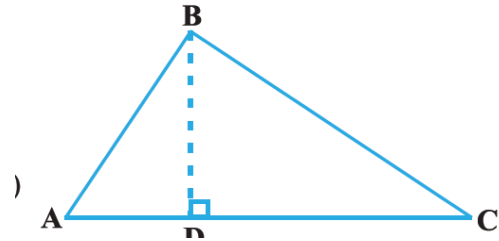
$$BC^2 = AC \times DC \text{ -----(2)}$$

Adding (1) and (2) we get.

$$\begin{aligned} AB^2 + BC^2 &= AC \times AD + AC \times DC \\ &= AC(AD + DC) \\ &= AC \times AC \end{aligned}$$

$$AB^2 + BC^2 = AC^2$$

$$AC^2 = AB^2 + BC^2$$



## GRAPH :

Ex: Solve by graph  $2x - 5y = -4$  and  $2x + y = 8$

Solution:  $2x - 5y = -4$

X	0	-2	3
Y	0.8	0	2

$$x = 0 : 2(0) - 5y = -4$$

$$-5y = -4$$

$$y = 4/5$$

$$y = 0.8$$

$$y = 0 : 2x - 5(0) = -4$$

$$2x = -4$$

$$x = -2$$

$$y = 2 : 2x - 5(2) = -4$$

$$2x = -4 + 10$$

$$x = 6/2$$

$$x = 3$$

$$2x + y = 8$$

X	0	4	3
Y	8	0	2

$$x = 0 : 2x + y = 8$$

$$2(0) + y = 8$$

$$y = 8$$

$$y = 0 : 2x + y = 8$$

$$2x + 0 = 8$$

$$2x = 8$$

$$x = 8/2$$

$$x = 4$$

$$y = 2 : 2x + (2) = 8$$

$$2x = 8 - 2$$

$$x = 6/2$$

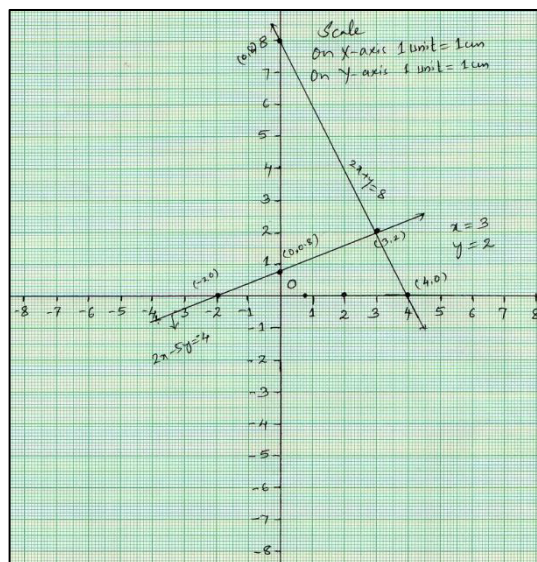
$$x = 3$$

$$2x - 5y = -4$$

$$2x + y = 8$$

$$-6y = -12$$

$$y = 2$$



Ex: Solve by graph  $x + 2y = -2$  and  $3x + 2y = 2$

Solution:  $x + 2y = -2$

X	0	-2	2
Y	-1	0	-2

$$x = 0 : x + 2y = -2$$

$$0 + 2y = -2$$

$$y = -1$$

$$y = 0 : x + 2y = -2$$

$$x + 2(0) = -2$$

$$x = -2$$

$$y = -2 : x + 2(-2) = -2$$

$$x - 4 = -2$$

$$x = -2 + 4$$

$$x = 2$$

$$3x + 2y = 2$$

X	0	0.6	2
Y	1	0	-2

$$x = 0 : 3x + 2y = 2$$

$$3(0) + 2y = 2$$

$$y = 1$$

$$y = 0 : 3x + 2y = 2$$

$$3x + 2(0) = 2$$

$$x = 2/3$$

$$x = 0.6$$

$$y = -2 : 3x + 2(-2) = 2$$

$$3x - 4 = 2$$

$$3x = 2 + 4$$

$$x = 2$$

$$y = -2 : 2x + 3(-2) = 2$$

$$2x = 2 + 6$$

$$x = 8/2$$

$$x = 4$$

$$x - 2y = 8$$

X	0	8	4
Y	-4	0	-2

$$x = 0 : 0 - 2y = 8$$

$$y = -4$$

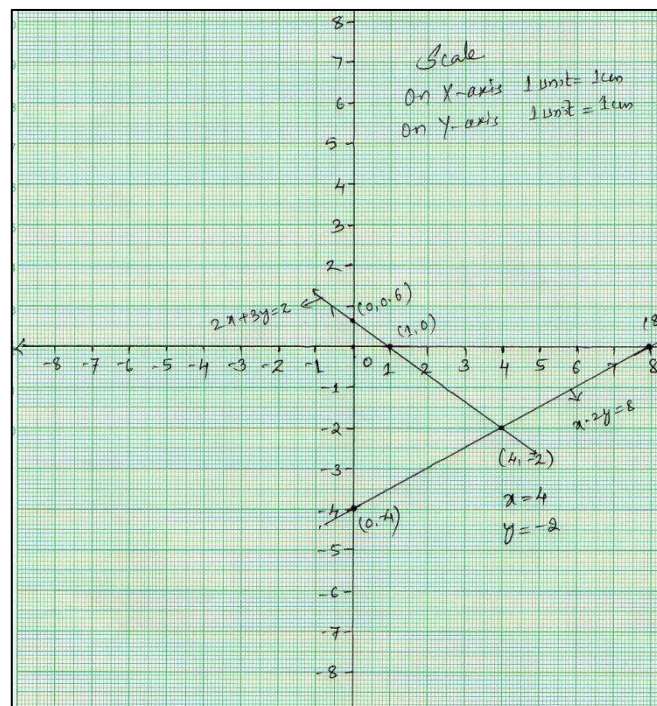
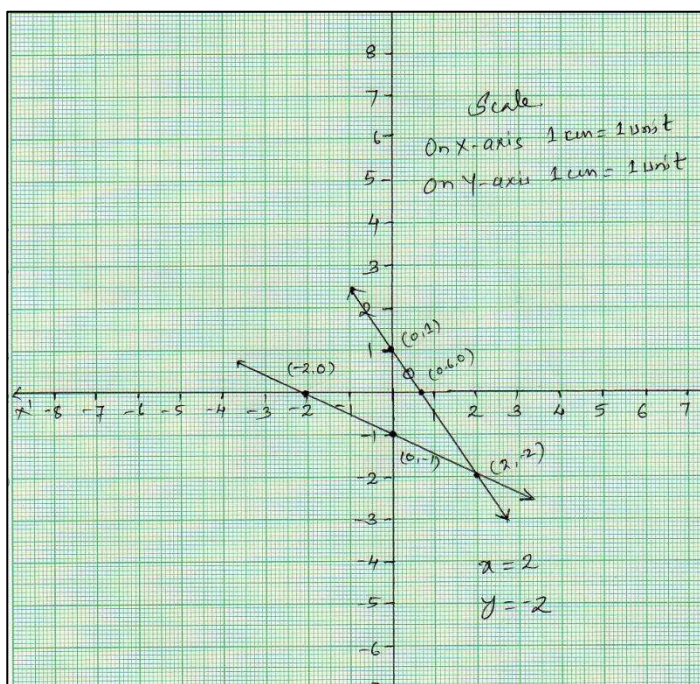
$$y = 0 : x - 2(0) = 8$$

$$x = 8$$

$$y = -2 : x - 2(-2) = 8$$

$$x = 8 - 4$$

$$x = 4$$



**Ex: Solve by graph  $2x + 3y = 2$  and  $x - 2y = 8$**

**Solution:**  $2x + 3y = 2$

X	0	1	4
Y	0.6	0	-2

$$x = 0 : 2(0) + 3y = 2$$

$$y = 2/3$$

$$y = 0.6$$

$$y = 0 : 2x + 3(0) = 2$$

$$2x = 2$$

$$x = 1$$

**Exercise:**

**Solve the following pair of linear equation by graphically method.**

- 1)  $2x + y - 6 = 0$  and  $4x - 2y - 4 = 0$
- 2)  $y = 2x - 2$  and  $y = 4x - 4$
- 3)  $x + 3y = 6$  and  $2x - 3y = 12$
- 4)  $x + 3y = 13$  and  $3x + y = 7$
- 5)  $x - y = -2$  and  $4x - y - 4 = 0$

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