## 2019

## MATHEMATICS QUESTION PAPERS FOR 10TH STD.

## MODEL QUESTION PAPER-1

Subject: Mathematics
Time : 3 hours

Subject code: 81E
Max.marks: 80
I. In the following questions four choices are given for each question chose and write correct answer along with its alphabet:

1. HCF of $6 \& 20$ is ....
a. 1
b. 30
c. 60
d. 2
2. If $\operatorname{Cos} A=\frac{1}{2}$, then the value of $\operatorname{Sin} A$ is.....
a. 4
b. $\frac{\sqrt{3}}{2}$
c. $\sqrt{3}$
d. 1
3. Secant touches the circle .... Times.
a. 2
b. 3
c. 4
d. 1
4. Which of the following formula to use to find the volume of cone.
a. $\frac{1}{3} \pi r^{2} h$
b. $\pi r^{2} h$
c. $4 \pi r^{3}$
d. $\frac{2}{3} \pi r^{2}$
5. If $a_{n}=4 n-2$, then the value of $a_{4}$ is....
a. 8
b. 14
c. 10
d. 6
6. In $\triangle L M N, \angle L=50^{\circ}$ and $\angle N=60^{\circ}$. If $\triangle L M N^{\sim} \triangle P Q R$, then find $\angle Q$.
a. $70^{\circ}$
b. $60^{\circ}$
b. $90^{\circ}$
d. $180^{\circ}$
7. The probability of sure event is
a. 0
b. 1
c. 0.5
d. 0.65
8. The roots of the equation $x 2+x-(p+1)=0$, where $p$ is a constant, are
a. $p, p+1$
b. $-p, p+1$
c. p. $-(p+1)$
d. $-p,-(p+1)$
II. Answer the following questions $1 \times 8=8$
9. Show that $x=-3$ is a solution of $x^{2}+6 x+9=0$.
10. Find the value of $k$ in which one root of the quadratic equation is $k x^{2}$ $14 x+8=0$ is six times the other.
11. If the $10^{\text {th }}$ term of an A.P is $20 \&$ common difference is 2 , then find the $4^{\text {th }}$ term.
12. State Pythagoras theorem.
13. Express 140 as its product of prime factors.
14. If $\sec A=\frac{15}{7}, \& A+B=90^{\circ}$, then find the value of $\operatorname{Cosec} B$.
15. Find: $\sin ^{2} 30^{\circ}+\cos ^{2} 60^{\circ}$.
16. Volume and surface area of the solid hemisphere are numerically equal. What is the diameter of the hemisphere?.
III. Answer the questions $2 \times 8=10$
17. Prove that $\sqrt{3}$ is an irrational number.
18. Solve $x+y=5 \& 2 x-y=7$.
19. Find the value of $p$, for which one root of the quadratic equation $p x^{2}-14 x+8=0$ is 6 times the other.
20. Find the distance between the points, $A(2 a, 6 a)$ and $B(2 a+\sqrt{3} a, 5 a)$.
21. $E$ is a point on the side $A D$ produced of a parallelogram $A B C D$ and $B E$ intersects $C D$ at $F$. Show that $\triangle A B E \sim \triangle C F B$.

OR
In the figure given below, $D E \| B C$. If $A D=2.4 \mathrm{~cm}, D B=3.6 \mathrm{~cm}$ and $A C=5 \mathrm{~cm}$ Find $A E$.

22. Two cubical dice whose faces are numbered from 1 to 6 are rolled simultaneously once. Find the probability that the sum of the two numbers occurring the top of the face is 6 .
23. Construct a pair of tangents to the circle of radius 4.5 cm from an external point 5.5 cm from the circle.
24. Find the value of $\operatorname{cosec} 30^{\circ}$, geometrically.
OR

If $A, B, C$ are interior angles of $\triangle A B C$, then show that $\cos \left(\frac{B+C}{2}\right)=\sin \frac{A}{2}$
25. A number consists of two digits. When the number is divided by the sum of its digits, the quotient is 7 . If 27 is subtracted from the number, the digits interchange their places. Find the number.

## OR

The sum of two numbers is 8 . Determine the numbers if the sum of their reciprocals is $\frac{8}{15}$.
26. If the polynomial $6 x^{4}+8 x^{3}-5 x^{2}+a x+b$ is exactly divisible by the polynomial $2 x^{2}-5$, then find the value of $a$ and $b$.
27. If the equation $\left(1+m^{2}\right) x^{2}+2 m c x+c^{2}-a^{2}=0$ has equal roots then show that $c^{2}=a^{2}\left(1+m^{2}\right)$.

## OR

If the sum of two natural numbers is 8 and their product is 15 , find the numbers.
28. The vertices of a triangle are $A(-1,3), B(1,-1)$ and $C(5,1)$. Find the length of the median through the vertex $C$.

OR
Find the coordinates of the points of trisection of the line segment joining the points $(3,-2)$ and $(-3,-4)$.
29. Prove that the tangents drawn from an external point to the circle are equal"
30. Three semicircles each of diameter 3 cm , a circle of diameter 4.5 cm and a semicircle of radius 4.5 cm are drawn in the given figure. Find the area of the shaded region.


OR

Find the area of the minor segment of a circle of radius 42 cm , if the length of the corresponding arc is 44 cm .
31. Draw less than ogive for the given data:

| C.I | $45-55$ | $55-65$ | $65-75$ | $75-85$ | $85-95$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| f | 3 | 10 | 11 | 8 | 3 |

32. Find the mean value for the given data:

| C.I | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| f | 3 | 5 | 9 | 5 | 3 |

33. Draw base $\mathrm{BC}=5 \mathrm{~cm}$, construct a triangle to it if $\mathrm{LABC}=60^{\circ}$, \& $\angle A C B=70^{\circ}$. Construct another triangle similar to it with $\frac{3}{5}$ th of the corresponding sides.
V. Solve

$$
4 \times 4=16
$$

34. Solve pair of linear equations graphically : $x-2 y=0$ \& $3 x+4 y=20$.
35. The sum of first six terms of an arithmetic progression is 42 . The ratio of its 10 th term to its 30 th term is $1: 3$. Calculate the first and the thirteenth term of the A.P.

## OR

The sum of the first sixteen terms of an A.P. is 112 and the sum of its next fourteen terms is 518. Find the A.P.
36. A moving boat is observed from the top of a 150 m high cliff moving away from the cliff. The angle of depression of the boat changes from $60^{\circ}$ to $45^{\circ}$ in 2 minutes. Find the speed of the boat in $m / h$.
37. State and prove B.P.T(Basic proportionality theorem).
VI. Solve the given problem $5 \times 1=5$
38. A toy is in the form of a hemisphere surmounted by a right circular cone of the same base radius as that of the hemisphere. If the radius of base of the cone is 21 cm and its volume is $\frac{2}{3}$ of the volume of the hemisphere, calculate the height of the cone and the surface area of the toy.

