

Model Question paper

Subject: Mathematics-2018-19

Model answers

Sl no	Answers	marks
1	C) $(x_1+x_2)/2, (y_1+y_2)/2$	1
2	C)3	1
3	C)0	1
4	A) $\frac{1}{3} \pi h(r_1^2 + r_2^2 + r_1 r_2)$	1
5	(D) 16 : 81	1
6	B)p/ $360 \times \pi r^2$	1
7	A) $(mx_2+nx_1)/m+n, (my_2+ny_1)/m+n$	1
8	A)Two distinct real	1
9	Equilateral	1
10	$OB^2 = BP^2 + OP^2$ $5^2 = BP^2 + 3^2$ $BP^2 = 25 - 9$ $BP^2 = 16$ $BP = 4\text{CM}$ Length of chord = $4+4 = 8\text{cm}$	1

11

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

1

$$\begin{array}{r} -5 \\ -1 \\ + \\ \hline \end{array} \quad \begin{array}{r} 7 \\ 3 \\ - \\ \hline \end{array}$$

$$\begin{array}{r} -4 \\ +4 \\ \hline \end{array}$$

$$d = \sqrt{(-4)^2 + (+4)^2}$$

$$d = \sqrt{16 + 16}$$

$$d = \sqrt{32} = d = 4\sqrt{2}$$

12

$$7 \times 11 \times 13.$$

1**13**

$$\begin{aligned} 50 &= 5 \times 2 \times 5 \\ &= 5^2 \times 2^1 \end{aligned}$$

1

therefore, $35/50$ has terminating decimal expansion

14

$$t^2 - 25$$

1

$$t^2 = 25$$

1

$$t = +5, t = -5$$

15

Numbers divisible by 3 between 0 to 99

	<p>3,6,9,-----99 $a=12$ $d=3$ $an=99$ $an = a + (n-1)d$ $99 = 12 + (n-1) 3$ $99 = 12 + 3n - 3$ $99 = 9 + 3n$ $90/3 = n$ $30 = n$ So, there are 30 two-digit numbers divisible by 3.</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
16	<p>In the figure $LM \parallel CB$ By basic proportionality Theorem $AM/MB = AL/LC$ ----- (1) $LN \parallel CD$ By basic proportionality Theorem $AN/AD = AL/LC$ ----- (2) By (1) and (2) We get $AM/MB = AN/AD$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
17	<p>$x + y = 14$ and $x - y = 4$ $x + y = 14$ $x - y = 4$ - + - ----- $2y = 10$ $y = 10/2 = 5$ $x + y = 14$ $X + 5 = 14$ $X = 14 - 5$ $X = 9$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
18	<p>Quadrant means centre angle 90 Circumference = $2\pi r$ $22 = 2\pi r$ $r = 22/2\pi$ Area of sector = $90/360 \times \pi \times r^2$</p>	$\frac{1}{2}$ $\frac{1}{2}$

	$\begin{aligned} &= \frac{1}{4} \times \pi \times 22 \times 22 / 2 \times 2 \times \pi \times \pi \\ &= \frac{1}{4} \times 121 \times 7/22 \\ &= 154/3 \text{ cm}^2 \end{aligned}$	$\frac{1}{2}$ $\frac{1}{2}$
19		$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
20	<p>Area of triangle = $\frac{1}{2} x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)$</p> $\begin{aligned} &= \frac{1}{2} 2 (0+4) -1(-4-3) +2(3-0) \\ &= \frac{1}{2} 2(4) -1(-7) + 2(3) \\ &= \frac{1}{2} (8 + 7 + 6) \\ &= \frac{1}{2} 21 \\ &= 21/2 \end{aligned}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
21	<p>Contradictory method Let us assume that $3 + 2\sqrt{5}$ is not a irrational number Then, $3 + 2\sqrt{5}$ is a rational number $3 + 2\sqrt{5} = a/b$ Here a and b are co-prime $\therefore b \neq 0$</p> <p>After simplification $3 - a/b = 2\sqrt{5}$ $1/2(3 - a/b) = \sqrt{5}$ $3/2 - a/2b = \sqrt{5}$ LHS is rational $= (3/2 - a/2b)$</p> <p>And RHS should be rational $= \sqrt{5}$ It gives rise to contradiction</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

	So $3 + 2\sqrt{5}$ irrational	$\frac{1}{2}$
22	<p>sum of zeroes = $-2 + (-5) = b/a$</p> $- (7) = -7/1$ $\frac{-7}{1} = -7$ <p>Product of zeroes = c/a</p> $(-2) \times (-5) = 10/1$ $10 = 10$	1
23	$2x^2 - 7x + 3 = 0$ $a = 2 \quad b = -7 \quad c = 3$ $X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $X = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(2)(3)}}{2(2)}$ $X = \frac{7 \pm \sqrt{49 - 24}}{4}$ $X = \frac{7 \pm \sqrt{25}}{4}$ $X = \frac{7+5}{4} = \frac{12}{4} = 3 \quad X = \frac{7-5}{4} = \frac{2}{4} = \frac{1}{2}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

28

$$\frac{2}{x} + \frac{3}{y} = 13, \frac{5}{x} - \frac{4}{y} = -2$$

$$\text{Put } \frac{2}{x} = p, \frac{1}{y} = q$$

$$2p + 3q = 13 \times 5$$

$$5p - 4q = -2 \times 2$$

$$\hline$$

$$10p + 15q = 65$$

$$10p - 8q = -4$$

$$\begin{array}{r} - \\ + \\ \hline \end{array}$$

$$23q = 69$$

$$q = 69/23$$

$$q = 3$$

$$5p - 4(3) = -2$$

$$5p - 12 = -2$$

$$5p = 10$$

$$P = 10/5 = 2$$

$$1/x = p = 2 \text{ so } x = 1/2$$

$$1/y = q = 5 \text{ so } y = 1/5$$

 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ **1****29**

$$\begin{array}{r} x^2 + 2x + 1) 3x^3 + x^2 + 2x + 5(3x - 5 \\ \quad \quad \quad 3x^3 + 6x^2 + 3x \end{array}$$

$$\begin{array}{r} - \\ - \\ - \end{array}$$

$$\hline$$

$$-5x^2 - x + 5$$

$$-5x^2 - 10x - 5$$

$$\begin{array}{r} + \\ + \\ + \end{array}$$

$$\hline$$

$$9x + 10$$

1**30**

Let AB be the height of the tower.

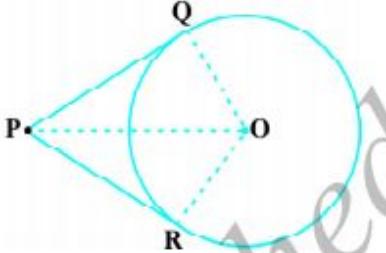
In ABC,

$$\tan 30^\circ = AB/BC$$

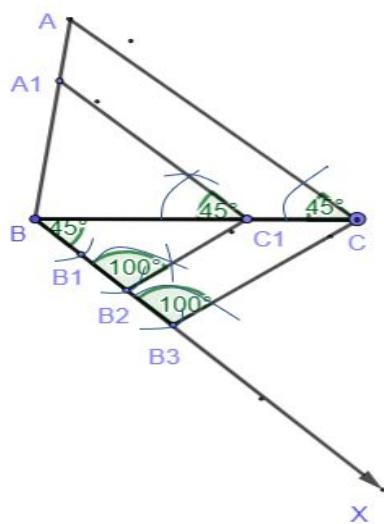
$$1/\sqrt{3} = AB/30$$

 $\frac{1}{2}$

	$AB = 30 / \sqrt{3}$ $AB = 30 \sqrt{3} / \sqrt{3} \times \sqrt{3}$ $AB = 30 \sqrt{3} / 3$ $AB = 10 / \sqrt{3}$ miters	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
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31	 <p>Given: O is the circle , P is a point lying outside the circle, PQ and PR are two tangents on the circle from P . To prove : PQ = PR. Construction:we join OP, OQ and OR</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
	statements	Reasons
	$\angle OQP = \angle ORP = 90^\circ$	angle between tangents and radius
	In right angled triangle triangles OQP and ORP $OQ = QR$ $OP = OP$ Therefore,, $\triangle OQP \cong \triangle ORP$	1 Radii of same circle common side RHS
	$PQ = PR$	CPCT

32

1
+
1
+
1

33

$$2x^2 + x + 4 = 0$$

On dividing the equation by 2

$$x^2 + x/2 + 4/2 = 0$$

$$x^2 + x/2 \times 1/4 = -2$$

On adding $\frac{1}{4}$ both sides

$$x^2 + x/2 \times \frac{1}{4} + (\frac{1}{4})^2 = -2 + (\frac{1}{4})^2$$

$$(x + \frac{1}{4})^2 = -2 + \frac{1}{16}$$

$$(x + \frac{1}{4})^2 = -\frac{31}{12}$$

There are no real roots

1

1

1

34

$$A + B + C = 180$$

$$B + C = 180 - A$$

$$(B + C)/2 = (180 - A)/2$$

$$(B + C)/2 = 90 - A/2$$

$$\sin(B + C)/2 = \sin(90 - A/2)$$

$$\sin(B + C)/2 = \cos A/2$$

1

1

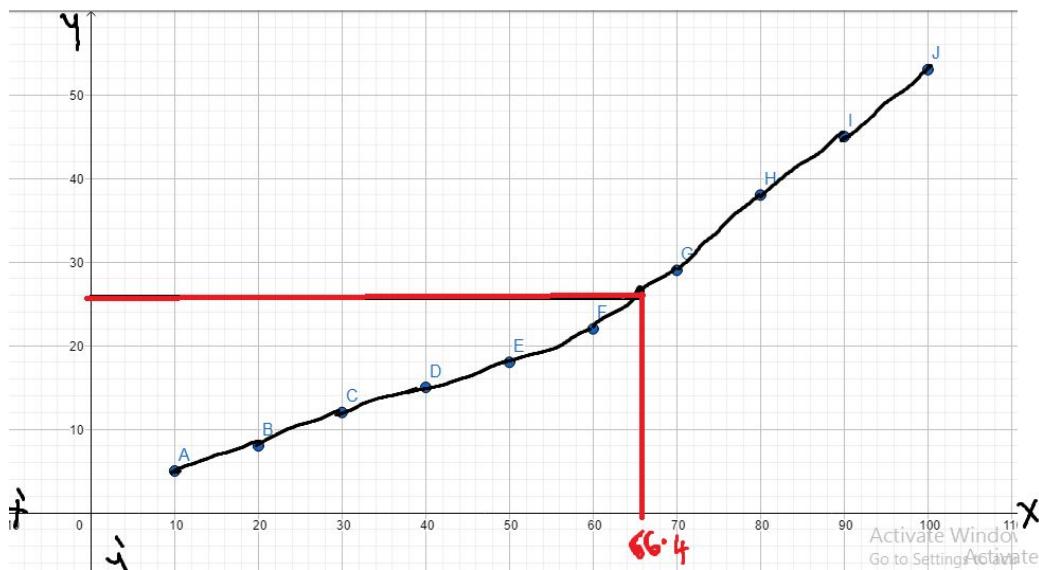
35	<table border="1"> <thead> <tr> <th>Cl</th><th>fi</th><th>xi</th><th>xifi</th><th></th></tr> </thead> <tbody> <tr> <td>0 - 2</td><td>1</td><td>0 1 2</td><td>1 X 1 = 1</td><td>$\bar{x} = \frac{\sum xifi}{\sum fi}$</td></tr> <tr> <td>2 - 4</td><td>2</td><td>2 3 4</td><td>3 X 2 = 6</td><td></td></tr> <tr> <td>4 - 6</td><td>1</td><td>4 5 6</td><td>5 X 1 = 5</td><td>$\bar{x} = \frac{162}{20}$</td></tr> <tr> <td>6 - 8</td><td>5</td><td>6 7 8</td><td>7 X 5 = 35</td><td></td></tr> <tr> <td>8 - 10</td><td>6</td><td>8 9 10</td><td>9 X 6 = 54</td><td></td></tr> <tr> <td>10 - 12</td><td>2</td><td>10 11 12</td><td>11 X 2 = 22</td><td></td></tr> <tr> <td>12 - 14</td><td>3</td><td>12 13 14</td><td>13 X 3 = 39</td><td></td></tr> <tr> <td></td><td>$\sum fi =$</td><td></td><td>$\sum xifi = 162$</td><td></td></tr> </tbody> </table>	Cl	fi	xi	xifi		0 - 2	1	0 1 2	1 X 1 = 1	$\bar{x} = \frac{\sum xifi}{\sum fi}$	2 - 4	2	2 3 4	3 X 2 = 6		4 - 6	1	4 5 6	5 X 1 = 5	$\bar{x} = \frac{162}{20}$	6 - 8	5	6 7 8	7 X 5 = 35		8 - 10	6	8 9 10	9 X 6 = 54		10 - 12	2	10 11 12	11 X 2 = 22		12 - 14	3	12 13 14	13 X 3 = 39			$\sum fi =$		$\sum xifi = 162$		1+1 +1
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36	<p>1) Less than method</p> <table border="1"> <thead> <tr> <th>Marks</th><th>Cl</th><th>No of students f</th><th>cf</th></tr> </thead> <tbody> <tr> <td>10</td><td></td><td>5</td><td>5</td></tr> <tr> <td>20</td><td></td><td>3</td><td>5 + 3 = 8</td></tr> <tr> <td>30</td><td></td><td>4</td><td>8 + 4 = 12</td></tr> <tr> <td>40</td><td></td><td>3</td><td>12 + 3 = 15</td></tr> <tr> <td>50</td><td></td><td>3</td><td>15 + 3 = 18</td></tr> <tr> <td>60</td><td></td><td>4</td><td>18 + 4 = 22</td></tr> <tr> <td>70</td><td></td><td>7</td><td>22 + 7 = 29</td></tr> <tr> <td>80</td><td></td><td>9</td><td>29 + 9 = 38</td></tr> <tr> <td>90</td><td></td><td>7</td><td>38 + 7 = 45</td></tr> </tbody> </table>	Marks	Cl	No of students f	cf	10		5	5	20		3	5 + 3 = 8	30		4	8 + 4 = 12	40		3	12 + 3 = 15	50		3	15 + 3 = 18	60		4	18 + 4 = 22	70		7	22 + 7 = 29	80		9	29 + 9 = 38	90		7	38 + 7 = 45	11/2					
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100

8

$$45 + 8 = 53$$

11/2



37

$$\text{nth term } a_n = a + (n-1)d$$

$$\text{4th term. } a_4 = a + 3d$$

$$\text{8th term } a_8 = a + 7d$$

$$a_4 + a_8 = 24$$

$$a + 3d + a + 7d = 24$$

$$2a + 10d = 24 \quad \dots \dots \dots (1)$$

$$\text{6th term. } a_6 = a + 5d$$

$$\text{10th term } a_{10} = a + 9d$$

$$a_6 + a_{10} = 24$$

$$a + 5d + a + 9d = 24$$

$$2a + 14d = 44 \quad \dots \dots \dots (2)$$

From (1) and (2)

$$2a + 10d = 24$$

$$2a + 14d = 44$$

- - -

$$-4d = -20$$

$$d = -20 / -4 = 5$$

Put $d = 5$ in (1)

$$2a + 10d = 24 \quad \dots \dots \dots (1)$$

1

1

1

	$2a + 10(5) = 24$ $2a + 50 = 24$ $2a = -26$ $a = -13$ $-13, -8, -3$	1
38	<p>Given: In $\triangle ABC$, if the line DE is drawn parallel to side BC of $\triangle ABC$ to intersect the AB and AC sides at distinct points D and E.</p> <p>To prove: $AD/DB = AE/EC$</p> <p>Construction: Join BE, and CD then Draw $DM \perp AC$, and $EN \perp AB$</p>	$1+$ $1+$ $1+$ 1

Proof:

	STATEMENTS	REASONS
1	In $\triangle ADE$, Area of $\triangle ADE = \frac{1}{2} AD \times EN$	Area of $\triangle = \frac{1}{2} \times \text{Base} \times \text{Height}$
	IN $\triangle BDE$, Area of $\triangle BDE = \frac{1}{2} DB \times EN$	Area of $\triangle = \frac{1}{2} \times \text{Base} \times \text{Height}$
	$\frac{\Delta ADE}{\Delta BDE} = \frac{\frac{1}{2} AD \times EN}{\frac{1}{2} DB \times EN}$ $= \frac{AD}{DB} \text{ ----- (1)}$	

	<p>Similarly, In ADE , Area of ADE = $\frac{1}{2}$ AE X DM</p>	<p>Area of Δ = $\frac{1}{2}$ X Base X Height</p>
	<p>In DEC Area of DEC = $\frac{1}{2}$ EC X DM</p>	<p>Area of Δ = $\frac{1}{2}$ X Base X Height</p>
	$\frac{\Delta ADE}{\Delta DEC} = \frac{\frac{1}{2} AE X DM}{\frac{1}{2} EC X DM}$ $= \frac{AE}{EC} \text{ ----- (2)}$	
	<p>Two triangles BDE And DEC are on the same base DE and between parallel lines BC and DE. so, ar(BDE) = ar(DEC))----- (3)</p>	
	<p>From (1),(2) AND (3) WE GET $AD/DB = AE/EC$</p>	

39

x	1	2	3
y	$5/3=1.6$	$4/3 =1.3$	1

x	1	2	3
y	$-10/3=-3.3$	$-8/3=-2.6$	$-6/3 =-2$

$$x+3y=6$$

$$3y=6-x$$

$$\begin{aligned} Y &= \frac{6-x}{3} & Y &= \frac{6-x}{3} & Y &= \frac{6-x}{3} \\ &= \frac{6-1}{3} & &= \frac{6-2}{3} & &= \frac{6-3}{3} \\ &= \frac{5}{3} & &= \frac{4}{3} & &= \frac{3}{3} \end{aligned}$$

$$2x -3y=12$$

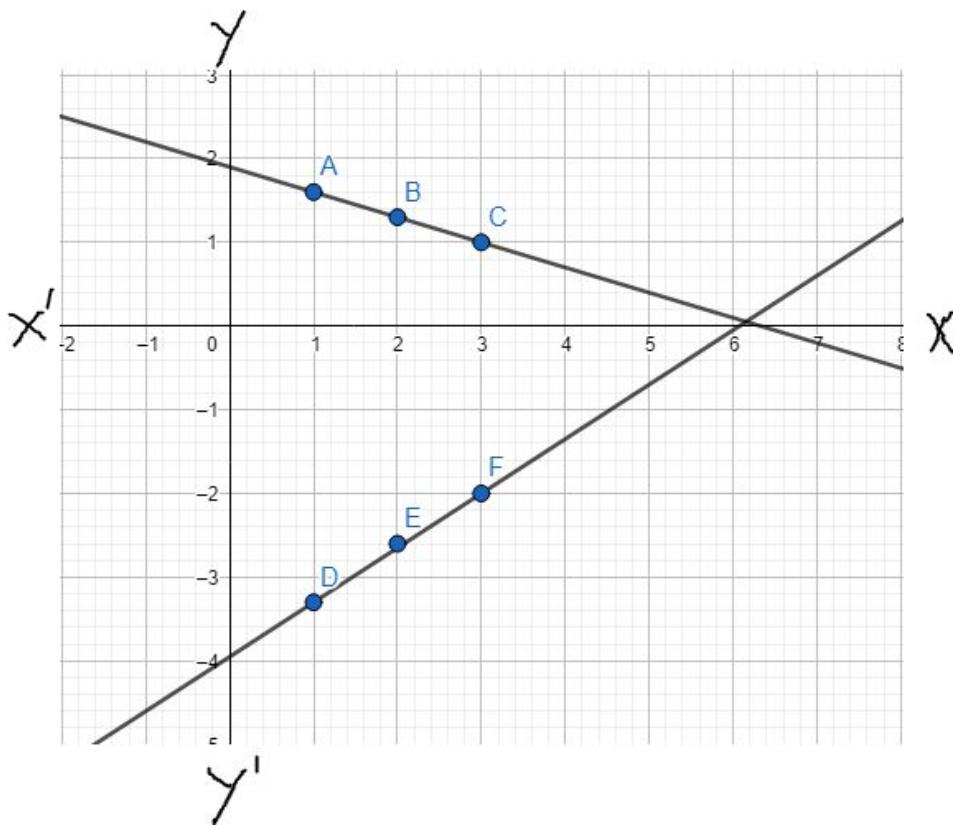
$$-3y=12-2x$$

$$Y = \frac{12-2x}{-3} \quad Y = \frac{12-2x}{-3} \quad Y = \frac{12-2x}{-3}$$

$$\begin{aligned} Y &= \frac{12-2(1)}{-3} & Y &= \frac{12-2(2)}{-3} & Y &= \frac{12-2(3)}{-3} \\ Y &= \frac{12-2}{-3} & Y &= \frac{12-4}{-3} & Y &= \frac{12-6}{-3} \\ Y &= \frac{10}{-3} & Y &= \frac{8}{-3} & Y &= \frac{6}{-3} \end{aligned}$$

1

1



2

40	<p>Two hemispheres and one cylinder are given Diameter of the capsule=5mm Therefore radius =$5/2 =2.5\text{mm}$ Length of the capsule=14mm Therefore length of the capsule =14mm Length of the cylinder =$14-(2.5+2.5)$ Surface area of the hemisphere=$2 \times 22/7 \times 2.5 \times 2.5 = 275/7 \text{mm}^2$ Surface area of the cylinder rh $= 2 \times 22/7 \times 2.5 \times 9$ $= 22/7 \times 45$ $= 990/7 \text{ mm}^2$ Required surface area of medicine capsule $= 2 \times \text{surface area of hemisphere} + \text{surface area of the cylinder}$ $= 2 \times 275/7 \times 990/7$ $= 550/7 + 990/7$ $= 1540/7 = 220\text{mm}^2$</p>	1 1 1 1